

For use in exams from the June 2017 Series onwards

DATA

FUNDAMENTAL CONSTANTS AND VALUES

Quantity	Symbol	Value	Units
speed of light in vacuo	c	3.00×10^8	m s^{-1}
permeability of free space	μ_0	$4\pi \times 10^{-7}$	H m^{-1}
permittivity of free space	ϵ_0	8.85×10^{-12}	F m^{-1}
magnitude of the charge of electron	e	1.60×10^{-19}	C
the Planck constant	h	6.63×10^{-34}	J s
gravitational constant	G	6.67×10^{-11}	$\text{N m}^2 \text{ kg}^{-2}$
the Avogadro constant	N_A	6.02×10^{23}	mol^{-1}
molar gas constant	R	8.31	$\text{J K}^{-1} \text{ mol}^{-1}$
the Boltzmann constant	k	1.38×10^{-23}	J K^{-1}
the Stefan constant	σ	5.67×10^{-8}	$\text{W m}^{-2} \text{ K}^{-4}$
the Wien constant	α	2.90×10^{-3}	m K
electron rest mass (equivalent to 5.5×10^{-4} u)	m_e	9.11×10^{-31}	kg
electron charge/mass ratio	$\frac{e}{m_e}$	1.76×10^{11}	C kg^{-1}
proton rest mass (equivalent to 1.00728 u)	m_p	$1.67(3) \times 10^{-27}$	kg
proton charge/mass ratio	$\frac{e}{m_p}$	9.58×10^7	C kg^{-1}
neutron rest mass (equivalent to 1.00867 u)	m_n	$1.67(5) \times 10^{-27}$	kg
gravitational field strength	g	9.81	N kg^{-1}
acceleration due to gravity	g	9.81	m s^{-2}
atomic mass unit (1u is equivalent to 931.3 MeV)	u	1.661×10^{-27}	kg

ASTRONOMICAL DATA

Body	Mass/kg	Mean radius/m
Sun	1.99×10^{30}	6.96×10^8
Earth	5.98×10^{24}	6.37×10^6

GEOMETRICAL EQUATIONS

arc length	$= r\theta$
circumference of circle	$= 2\pi r$
area of circle	$= \pi r^2$
surface area of cylinder	$= 2\pi rh$
area of sphere	$= 4\pi r^2$
volume of sphere	$= \frac{4}{3}\pi r^3$

Particle Physics

Class	Name	Symbol	Rest energy/MeV
photon	photon	γ	0
lepton	neutrino	ν_e	0
		ν_μ	0
	electron	e^\pm	0.510999
	muon	μ^\pm	105.659
mesons	π meson	π^\pm	139.576
		π^0	134.972
K meson	K meson	K^\pm	493.821
		K^0	497.762
baryons	proton	p	938.257
	neutron	n	939.551

Properties of quarks

antiquarks have opposite signs

Type	Charge	Baryon number	Strangeness
u	$+\frac{2}{3}e$	$+\frac{1}{3}$	0
d	$-\frac{1}{3}e$	$+\frac{1}{3}$	0
s	$-\frac{1}{3}e$	$+\frac{1}{3}$	-1

Properties of Leptons

Lepton number		
Particles:	e^- , ν_e ; μ^- , ν_μ	+ 1
Antiparticles:	e^+ , $\bar{\nu}_e$, μ^+ , $\bar{\nu}_\mu$	- 1

Protons and energy levels

photon energy	$E = hf = hc/\lambda$
photoelectricity	$hf = \phi + E_{k(\max)}$
energy levels	$hf = E_1 - E_2$
de Broglie Wavelength	$\lambda = \frac{h}{p} = \frac{h}{mv}$

Waves

wave speed	$c = f\lambda$	period	$f = \frac{1}{T}$
first harmonic	$f = \frac{1}{2l}\sqrt{\frac{T}{\mu}}$		
fringe spacing	$w = \frac{\lambda D}{s}$	diffraction grating	$d \sin \theta = n\lambda$
refractive index of a substance s,	$n = \frac{c}{c_s}$		
for two different substances of refractive indices n_1 and n_2 ,			
law of refraction	$n_1 \sin \theta_1 = n_2 \sin \theta_2$		
critical angle	$\sin \theta_c = \frac{n_2}{n_1}$ for $n_1 > n_2$		

Mechanics

moments	moment = Fd		
velocity and acceleration	$v = \frac{\Delta s}{\Delta t}$	$a = \frac{\Delta v}{\Delta t}$	
equations of motion	$v = u + at$	$s = \left(\frac{u+v}{2}\right)t$	
	$v^2 = u^2 + 2as$	$s = ut + \frac{at^2}{2}$	
force	$F = ma$		
force	$F = \frac{\Delta(mv)}{\Delta t}$		
impulse	$F \Delta t = \Delta(mv)$		
work, energy and power	$W = F s \cos \theta$		
	$E_k = \frac{1}{2} m v^2$	$\Delta E_p = mg\Delta h$	
	$P = \frac{\Delta W}{\Delta t}$, $P = Fv$		
efficiency	$\text{efficiency} = \frac{\text{useful output power}}{\text{input power}}$		

Materials

density	$\rho = \frac{m}{V}$	Hooke's law	$F = k \Delta L$
Young modulus	$= \frac{\text{tensile stress}}{\text{tensile strain}}$	tensile stress	$= \frac{F}{A}$
		tensile strain	$= \frac{\Delta L}{L}$
energy stored	$E = \frac{1}{2} F \Delta L$		

Electricity

<i>current and pd</i>	$I = \frac{\Delta Q}{\Delta t}$	$V = \frac{W}{Q}$	$R = \frac{V}{I}$
<i>resistivity</i>	$\rho = \frac{RA}{L}$		
<i>resistors in series</i>	$R_T = R_1 + R_2 + R_3 + \dots$		
<i>resistors in parallel</i>	$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$		
<i>power</i>	$P = VI = I^2R = \frac{V^2}{R}$		
<i>emf</i>	$\varepsilon = \frac{E}{Q}$	$\varepsilon = I(R + r)$	

Circular motion

<i>magnitude of angular speed</i>	$\omega = \frac{v}{r}$
	$\omega = 2\pi f$
<i>centripetal acceleration</i>	$a = \frac{v^2}{r} = \omega^2 r$
<i>centripetal force</i>	$F = \frac{mv^2}{r} = m\omega^2 r$

Simple harmonic motion

<i>acceleration</i>	$a = -\omega^2 x$
<i>displacement</i>	$x = A \cos(\omega t)$
<i>speed</i>	$v = \pm \omega \sqrt{(A^2 - x^2)}$
<i>maximum speed</i>	$v_{max} = \omega A$
<i>maximum acceleration</i>	$a_{max} = \omega^2 A$
<i>for a Mass-spring system</i>	$T = 2\pi \sqrt{\frac{m}{k}}$
<i>for a simple pendulum</i>	$T = 2\pi \sqrt{\frac{l}{g}}$

Thermal physics

<i>energy to change temperature</i>	$Q = mc\Delta\theta$
<i>energy to change state</i>	$Q = m l$
<i>gas law</i>	$pV = nRT$
	$pV = NkT$
<i>kinetic theory model</i>	$pV = \frac{1}{3}N m (c_{rms})^2$
<i>kinetic energy of gas molecule</i>	$\frac{1}{2}m (c_{rms})^2 = \frac{3}{2}kT = \frac{3RT}{2N_A}$

Gravitational fields

<i>force between two masses</i>	$F = \frac{Gm_1m_2}{r^2}$
<i>gravitational field strength</i>	$g = \frac{F}{m}$
<i>magnitude of gravitational field strength in a radial field</i>	$g = \frac{GM}{r^2}$
<i>work done</i>	$\Delta W = m\Delta V$
<i>gravitational potential</i>	$V = -\frac{GM}{r}$
	$g = -\frac{\Delta V}{\Delta r}$

Electric fields and capacitors

<i>force between two point charges</i>	$F = \frac{1}{4\pi\epsilon_0} \frac{Q_1Q_2}{r^2}$
<i>force on a charge</i>	$F = EQ$
<i>field strength for a uniform field</i>	$E = \frac{V}{d}$
<i>work done</i>	$\Delta W = Q\Delta V$
<i>field strength for a radial field</i>	$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$
<i>electric potential</i>	$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$
	$E = \frac{\Delta V}{\Delta r}$
<i>capacitance</i>	$C = \frac{Q}{V}$
	$C = \frac{A\epsilon_0\epsilon_r}{d}$
<i>capacitor energy stored</i>	$E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}$
<i>capacitor charging</i>	$Q = Q_0(1 - e^{-t/RC})$
<i>decay of charge</i>	$Q = Q_0e^{-t/RC}$
<i>time constant</i>	RC

Magnetic fields

<i>force on a current</i>	$F = BIl$
<i>force on a moving charge</i>	$F = BQv$
<i>magnetic flux</i>	$\Phi = BA$
<i>magnetic flux linkage</i>	$N\Phi = BAN \cos \theta$
<i>magnitude of induced emf</i>	$\varepsilon = N \frac{\Delta\Phi}{\Delta t}$
	$N\Phi = BAN \cos \theta$
<i>emf induced in a rotating coil</i>	$\varepsilon = BAN\omega \sin \omega t$
<i>alternating current</i>	$I_{\text{rms}} = \frac{I_0}{\sqrt{2}}$ $V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$
<i>transformer equations</i>	$\frac{N_s}{N_p} = \frac{V_s}{V_p}$
	$\text{efficiency} = \frac{I_s V_s}{I_p V_p}$

OPTIONS

Astrophysics

1 astronomical unit = 1.50×10^{11} m
1 light year = 9.46×10^{15} m
1 parsec = 206265 AU = 3.08×10^{16} m
= 3.26 light years

Hubble constant, H = 65 km s⁻¹ Mpc⁻¹

$M = \frac{\text{angle subtended by image at eye}}{\text{angle subtended by object at unaided eye}}$
<i>in normal adjustment</i> $M = \frac{f_0}{f_e}$
<i>Rayleigh criterion</i> $\theta \approx \frac{\lambda}{D}$
<i>magnitude equation</i> $m - M = 5 \log \frac{d}{10}$

Nuclear physics

<i>the inverse square law for γ radiation</i>	$I = \frac{k}{x^2}$
<i>radioactive decay</i>	$\frac{\Delta N}{\Delta t} = -\lambda N, N = N_0 e^{-\lambda t}$
<i>activity</i>	$A = \lambda N$
<i>half-life</i>	$T_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$
<i>nuclear radius</i>	$R = R_0 A^{1/3}$
<i>energy-mass equation</i>	$E = mc^2$

<i>Wien's law</i>	$\lambda_{\text{max}} T = 2.9 \times 10^{-3}$ m K
<i>Stefan's law</i>	$P = \sigma AT^4$
<i>Schwarzschild radius</i>	$R_s \approx \frac{2GM}{c^2}$
<i>Doppler shift for $v \ll c$</i>	$z = \frac{\Delta f}{f} = -\frac{\Delta\lambda}{\lambda} = \frac{v}{c}$
<i>Hubble's law</i>	$v = Hd$

Medical physics

<i>lens equations</i>	$P = \frac{1}{f}$ $m = \frac{v}{u}$ $\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$
<i>threshold of hearing</i>	$I_0 = 1.0 \times 10^{-12}$ W m ⁻²
<i>intensity level</i>	$\text{intensity level} = 10 \log \frac{I}{I_0}$
<i>absorption</i>	$I = I_0 e^{-\mu x}$ $\mu_m = \frac{\mu}{\rho}$
<i>ultrasound imaging</i>	$Z = p c$ $\frac{I_t}{I_i} = \left(\frac{Z_2 - Z_1}{Z_2 + Z_1} \right)^2$
<i>half-lives</i>	$\frac{1}{T_E} = \frac{1}{T_B} + \frac{1}{T_P}$

Engineering physics

<i>moment of inertia</i>	$I = \Sigma mr^2$
<i>angular kinetic energy</i>	$E_k = \frac{1}{2}I\omega^2$
<i>equations of angular motion</i>	$\omega_2 = \omega_1 + \alpha t$ $\omega_2^2 = \omega_1^2 + 2\alpha\theta$ $\theta = \omega_1 t + \frac{\alpha t^2}{2}$ $\theta = \frac{(\omega_1 + \omega_2) t}{2}$
<i>torque</i>	$T = I \alpha$ $T = F r$
<i>angular momentum</i>	$angular momentum = I\omega$
<i>angular impulse</i>	$T\Delta t = \Delta(I\omega)$
<i>work done</i>	$W = T\theta$
<i>power</i>	$P = T\omega$
<i>thermodynamics</i>	$Q = \Delta U + W$ $W = p\Delta V$
<i>adiabatic change</i>	$pV^\gamma = \text{constant}$
<i>isothermal change</i>	$pV = \text{constant}$
<i>heat engines</i>	
<i>efficiency</i>	$\text{efficiency} = \frac{W}{Q_H} = \frac{Q_H - Q_C}{Q_H}$
<i>maximum theoretical efficiency</i>	$\text{efficiency} = \frac{T_H - T_C}{T_H}$
<i>work done per cycle</i>	= area of loop
<i>input power</i>	= calorific value \times fuel flow rate
<i>indicated power</i>	= (area of $p - V$ loop) \times (number of cycles per second) \times (number of cylinders)
<i>output or brake power</i>	$P = T\omega$
<i>friction power</i>	= indicated power - brake power
<i>heat pumps and refrigerators</i>	
<i>refrigerator</i> : $COP_{\text{ref}} = \frac{Q_C}{W} = \frac{Q_C}{Q_H - Q_C}$	
<i>heat pump</i> : $COP_{\text{hp}} = \frac{Q_H}{W} = \frac{Q_H}{Q_H - Q_C}$	

Turning points in physics

<i>electrons in fields</i>	$F = \frac{eV}{d}$ $F = Bev$ $r = \frac{mv}{Be}$ $\frac{1}{2}mv^2 = eV$ $\frac{QV}{d} = mg$ $F = 6\pi\eta rv$
<i>Millikan's experiment</i>	
<i>Maxwell's formula</i>	$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$
	$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2meV}}$
<i>special relativity</i>	$t = \frac{t_0}{\sqrt{1 - \frac{v^2}{c^2}}}$ $l = l_0 \sqrt{1 - \frac{v^2}{c^2}}$
	$E = mc^2 = \frac{m_0 c^2}{\sqrt{1 - \frac{v^2}{c^2}}}$

Electronics

<i>resonant frequency</i>	$f_0 = \frac{1}{2\pi \sqrt{LC}}$
<i>Q-factor</i>	$Q = \frac{f_0}{f_B}$
<i>operational amplifiers</i> :	
<i>open loop</i>	$V_{\text{out}} = A_{OL}(V_+ - V_-)$
<i>inverting amplifier</i>	$\frac{V_{\text{out}}}{V_{\text{in}}} = -\frac{R_f}{R_{\text{in}}}$
<i>non-inverting amplifier</i>	$\frac{V_{\text{out}}}{V_{\text{in}}} = 1 + \frac{R_f}{R_1}$
<i>summing amplifier</i>	$V_{\text{out}} = -R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} + \dots \right)$
<i>difference amplifier</i>	$V_{\text{out}} = (V_+ - V_-) \frac{R_f}{R_1}$
<i>Bandwidth requirement</i> :	
<i>for AM</i>	$\text{bandwidth} = 2f_M$
<i>for FM</i>	$\text{bandwidth} = 2(\Delta f + f_M)$