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| **Q** | Scheme | Marks | AOs | Pearson Progression Step and Progress Descriptor |
| **1a** | *X* ~ Po(3) | **B1** | 3.3 | 3rd  Use the Poisson distribution to model real-world situations |
| P(*X* > 4) = 1 − P(*X* ⩽ 4) = 1 − 0.8153 | **M1** | 1.1b |
| = 0.1847 | **A1** | 1.1b |
|  | **(3)** |  |  |
| **1b** | Expectation = 3, Variance = 3 (need both) | **B1** | 1.1a | 4th  Calculate the mean of a Poisson distribution |
|  | **(1)** |  |  |
| **1c** | P(*X* ⩽ *x*) ⩾ 0.95  P(*X* ⩽ 5) = 0.9161  P(*X* ⩽ 6) = 0.9665 | **M1**  **A1** | 1.1b  1.1b | 3rd  Use the Poisson distribution to model real-world situations |
| The newsagent should order six copies in order to meet the demand with a probability of at least 0.95 | **A1** | 2.4 |
|  | **(3)** |  |  |
| **(7 marks)** | | | | |
| **Notes** | | | | |

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| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress Descriptor |
| **2a** | Expectation = 150 × 0.015 = 2.25 | **B1** | 1.1b | 4th  Calculate the variance of a binomial distribution |
| Variance = 150 × 0.015 × 0.985 = 2.21625 | **B1** | 1.1b |
|  | **(2)** |  |  |
| **2b** | Expectation ≈ Variance | **B1** | 2.4 | 6th  Understand when to use a Poisson distribution as an approximation to the binomial distribution |
|  | **(1)** |  |  |
| **2c** | *X* ~ Po(2.25) | **B1** | 3.3 | 6th  Use the Poisson distribution as an approximation to the binomial distribution |
| P(*X* > 5) = 1 – P(*X* ⩽ 5) | **M1** | 1.1b |
| = 0.0274 | **A1** | 1.1b |
|  | **(3)** |  |  |
| (6 marks) | | | | |
| Notes | | | | |

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| **Q** | **Scheme** | **Marks** | **AOs** | **Pearson Progression Step and Progress Descriptor** |
| **3a** | *X* ~ Po(3.6) | **B1** | 3.3 | 6th  Understand when to use a Poisson distribution as an approximation to the binomial distribution |
| *p* is small and *n* is large (*np* < 10) | **B1** | 2.4 |
|  | **(2)** |  |  |
| **3b** | P(*X* ⩽ 3) | **M1** | 1.1b | 6th  Use the Poisson distribution as an approximation to the binomial distribution |
| = 0.5152 | **A1** | 1.1b |
|  | **(2)** |  |  |
| **3c** | *Y* ~ B(10, 0.5152) | **B1** | 3.3 | 5th  Solve problems involving the mean and variance of a binomial distribution |
| Mean = *np* = 5.152 | **B1** | 1.1b |
| Variance = *npq* = 2.4976896… | **M1** | 1.1b |
| Standard deviation =  = 1.5804… = 1.58 (3 s.f.) | **A1** | 1.1b |
|  | **(4)** |  |  |
| **(8 marks)** | | | | |
| **Notes**  **3a** Accept ‘Poisson’ without stated *λ* if correct value used in **b** | | | | |

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| **Q** | **Scheme** | **Marks** | **AOs** | **Pearson Progression Step and Progress Descriptor** |
| **4a** | H0: *λ* = 1.5; H1: *λ* < 1.5 | **B1** | 2.5 | 3rd  Understand the language of hypothesis testing |
|  | **(1)** |  |  |
| **4b** | *X* ~ Po(9) | **B1** | 3.3 | 4th  Carry out one-tailed tests for the mean of a Poisson distribution |
| P(*X* ⩽ 3) = 0.0212  P(*X* ⩽ 4) = 0.0550 | **M1** | 1.1b |
| Hence critical region is 3 or fewer | **A1** | 1.1b |
|  | **(3)** |  |  |
| **4c** | 0.0212 | **B1** | 1.1a | 3rd  Understand the language of hypothesis testing |
|  | **(1)** |  |  |
| **4d** | 4 is not in the critical region … | **B1** | 2.2b | 4th  Carry out one-tailed tests for the mean of a Poisson distribution |
| … so accept the null hypothesis: there is no evidence of a reduction in the (average) number of errors. | **B1** | 2.2b |
|  |  | **(2)** |  |  |
| **(7 marks)** | | | | |
| **Notes**  **4a** Accept hypotheses framed with *λ* = 9 | | | | |

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| **Q** | **Scheme** | **Marks** | **AOs** | **Pearson Progression Step and Progress Descriptor** |
| **5a** | *X* ~ Po(4.7) | **B1** | 3.3 | 4th  Understand the additive property of the Poisson distribution |
| P(*X* ⩾ 9) = 1 − P(*X* ⩽ 8) = 1 – 0.9497 | **M1** | 1.1b |
| = 0.0503 | **A1** | 1.1b |
|  | **(3)** |  |  |
| **5b** | H0: *λ* = 4.7; H1: *λ* ≠ 4.7 | **B1** | 2.5 | 5th  Carry out two-tailed tests for the mean of a Poisson distribution |
| 0.0503 > 0.05 | **M1** | 1.1b |
| Therefore, accept null hypothesis | **A1** | 2.2b |
| There is no evidence that the number of cars and vans passing the recording point has changed | **A1** | 2.2b |
|  | **(4)** |  |  |
| **(7 marks)** | | | | |
| **Notes**  **5b** Accept ft their part **a** if conclusions are consistent and in context | | | | |