

**C1****DIFFERENTIATION****Worksheet B**1 Differentiate with respect to  $x$ 

a  $x^2$

b  $x^4$

c  $x$

d  $x^9$

e  $x^{-3}$

f  $x^{-1}$

g  $4x^2$

h  $7x$

i  $2x^5$

j  $3$

k  $8x^{-2}$

l  $11x^{-4}$

2 Find  $\frac{dy}{dx}$ 

a  $y = x^5 + x^2$

b  $y = x + x^3$

c  $y = x^4 + 2$

d  $y = x^6 - 2x$

e  $y = 6x^3 + 5x^{-2}$

f  $y = x^2 - 4x + 1$

g  $y = x^{-1} - x^{-5}$

h  $y = 4x^3 + 3x^{-4}$

3 Differentiate with respect to  $t$ 

a  $t^6$

b  $5t^{-3}$

c  $t^{\frac{1}{2}}$

d  $t^{\frac{2}{3}}$

e  $\frac{3}{4}t^2$

f  $8t^{\frac{1}{4}}$

g  $2t^{\frac{7}{2}}$

h  $t^{-\frac{1}{5}}$

i  $\frac{1}{2}t^{\frac{6}{5}}$

j  $t^{-\frac{3}{2}}$

k  $12t^{-\frac{5}{4}}$

l  $\frac{1}{6}t^{\frac{4}{3}}$

4 Find  $f'(x)$ 

a  $f(x) = 2x + \frac{1}{3}x^6$

b  $f(x) = x^{\frac{3}{2}} - 5$

c  $f(x) = x + 4x^{\frac{1}{2}}$

d  $f(x) = 6x^{\frac{5}{3}} - x^{-4}$

e  $f(x) = 7 + x^{-\frac{4}{5}}$

f  $f(x) = 2x^{\frac{1}{6}} + x^{\frac{3}{4}}$

g  $f(x) = 3x^{-1} - 5x^{-\frac{3}{2}}$

h  $f(x) = 2 - 7x^{-1} + x^{-\frac{8}{3}}$

5 Find  $\frac{dy}{dx}$ 

a  $y = \sqrt{x}$

b  $y = 4 - \frac{1}{x}$

c  $y = 3x^2 + \sqrt[3]{x}$

d  $y = 9x + \frac{3}{x}$

e  $y = \frac{1}{4x} - \frac{1}{x^2}$

f  $y = \frac{6}{\sqrt[4]{x}}$

g  $y = \sqrt{x^5}$

h  $y = 8\sqrt{x} + \frac{4}{3x^2}$

6 Find  $\frac{ds}{dt}$ 

a  $s = t(t+3)$

b  $s = (t-2)^2$

c  $s = 5t(t^3 + 4t)$

d  $s = t^2(7t - t^{-1})$

e  $s = (t+1)(t+6)$

f  $s = (t-4)(t+2)$

g  $s = t(t^4 + 3t^2 + 9)$

h  $s = t(t-1)(2t-3)$

7 Find  $\frac{dy}{dx}$ 

a  $y = \sqrt{x}(x-4)$

b  $y = \frac{x^3 - 2x}{x}$

c  $y = \frac{4x^3 + x}{x^2}$

d  $y = \frac{x+3}{\sqrt{x}}$

e  $y = \frac{4-x^3}{2x}$

f  $y = \frac{5+\sqrt{x}}{x^2}$

g  $y = \frac{9x-2}{3x}$

h  $y = \frac{8x+x^3}{4\sqrt{x}}$

8 In each case, find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$ .

a  $y = 4x^2 - x + 3$

b  $y = x^3 + 5x^2 + 2x - 6$

c  $y = 8 - \frac{2}{x}$

d  $y = 2x^4 + 3x^2 - 9$

e  $y = \frac{3x^6 - 4}{x^2}$

f  $y = 6x^{\frac{1}{2}} - x^{-\frac{1}{2}}$