

## Mechanics 19 – Statics 1

Please **complete** this homework by \_\_\_\_\_. Start it early. If you can't do a question you will then have time to ask your teacher for help or go to a drop in session.

### Section 1 – Review of previous topics. Please complete all questions.

1. A uniform beam AB of mass 40 kg and length 3 m, rests on two supports, one at A and the other at C, where  $BC = 1$  m, as shown.



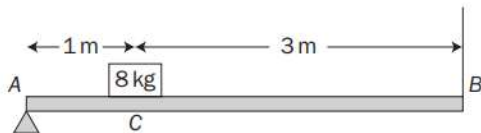
A load of mass 10 kg is attached to the beam at B.

- Draw a diagram showing the forces acting on the beam.
- Calculate the magnitude of the reaction forces at A and C.

The load at B is now increased to  $m$  kg, as a result of which the beam is on the point of tipping about C.

- Calculate  $m$ .

2. A uniform beam AB of mass 20 kg and length 4 m rests on a support at A and is held in a horizontal position by a vertical string attached to the beam at B. A load of mass 8 kg is placed on the beam at C, where  $AC = 1$  m.



- Calculate the reaction at the support at A.
  - Find the tension in the string.

The string has a breaking strain of 170 N.

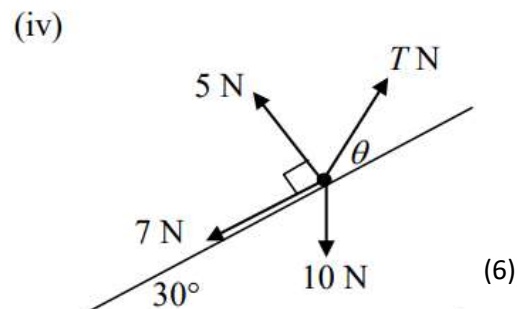
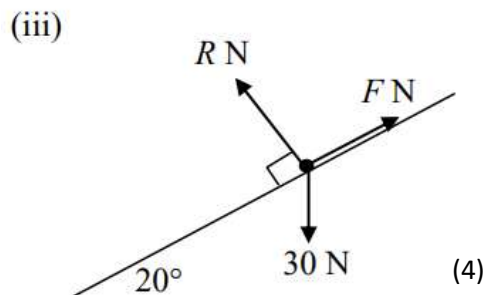
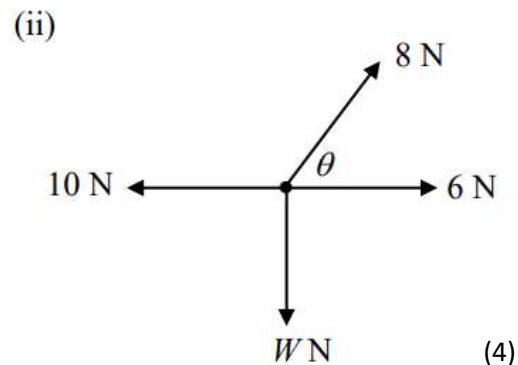
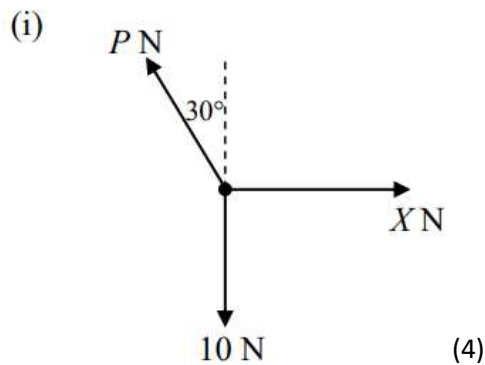
- How close to B could the 8 kg load be moved without breaking the string?

3. A random sample of daily rainfall figures is taken from the data from Leeming in 1987. The values obtained are: 0.5, 0.8, 11.5, 0.5, 1.5, 0.8, 21.6, 1.2, 1.2, 1.5, 0.8, 1.5, 12.6, 16.8, 0.9.
- An outlier is defined as a value which is more than 1.5 times the interquartile range above  $Q_3$  or more than 1.5 times the interquartile range below  $Q_1$ . Determine which values, if any, are outliers.
  - Using your knowledge of the data set, would you expect a sample of the same size from the data for Perth to be more likely or less likely to contain an outlier? You must give a reason for your answer.

Section 2 – Consolidation of this week’s topic. Please complete all questions.

1.

Each of the diagrams below shows a particle in equilibrium under the action of various forces. In each case find the values of the unknown forces and angles.

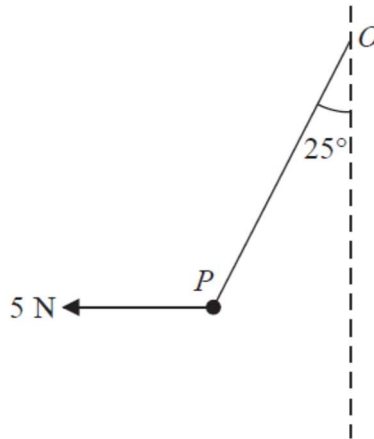


**(18 marks)**

- A particle of mass 5kg is suspended in equilibrium by two light inextensible strings which make angles of  $30^\circ$  and  $45^\circ$  respectively with the horizontal. Find the tensions in the strings **(8 marks)**
- A particle of weight 40 N is attached to the end of a light inextensible string of length 2 m. The other end of the string is attached to a vertical wall. The particle is held at a distance of 1.2 m from the wall by a horizontal force F. Find the magnitude of F and the tension in the string. **(7 marks)**
- A small weight of 20 N is at rest on a smooth plane inclined at  $30^\circ$  to the horizontal. It is held in position by a light rope. The angle between the rope and the plane is  $20^\circ$ . Find the tension in the rope and the reaction at the plane. **(7 marks)**

**(7 marks)**

5. A particle  $P$  of weight  $W$  newtons is attached to one end of a light inextensible string. The other end of the string is attached to a fixed point  $O$ . A horizontal force of magnitude  $5\text{ N}$  is applied to  $P$ . The particle  $P$  is in equilibrium with the string taut and with  $OP$  making an angle of  $25^\circ$  to the downward vertical, as shown in Figure 1.



**Figure 1**

Find

- (a) the tension in the string,

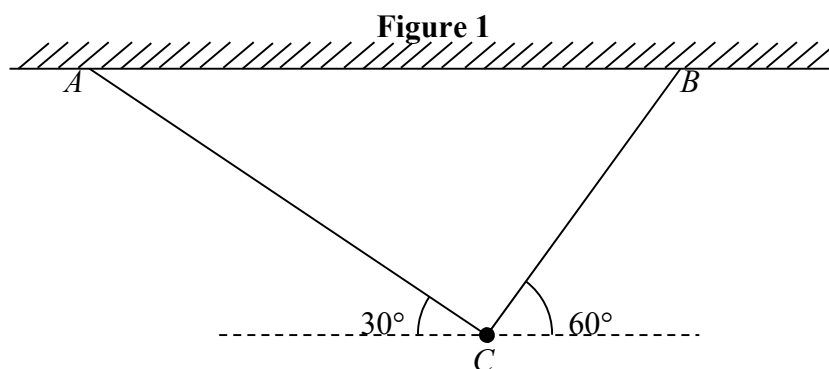
(3)

- (b) the value of  $W$ .

(3)

**(6 marks)**

6.



**Figure 1**

A particle of weight  $W$  newtons is attached at  $C$  to the ends of two light inextensible strings  $AC$  and  $BC$ . The other ends of the strings are attached to two fixed points  $A$  and  $B$  on a horizontal ceiling. The particle hangs in equilibrium with  $AC$  and  $BC$  inclined to the horizontal at  $30^\circ$  and  $60^\circ$  respectively, as shown in Fig.1. Given the tension in  $AC$  is  $50\text{ N}$ , calculate

- (a) the tension in  $BC$ , to 3 significant figures,

(3)

- (b) the value of  $W$ .

(3)

**(6 marks)**

**TOTAL 52 marks**