

## Mechanics 7 – Connected Particles

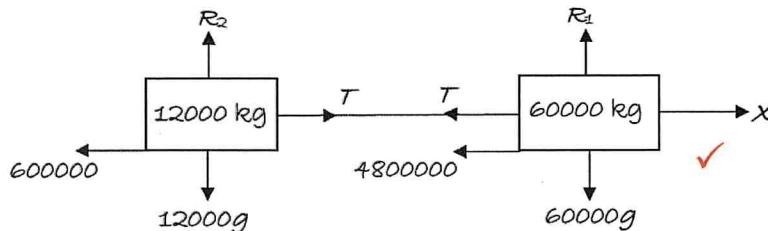
### Section 1

- (a)  $\mathbf{v} = 6\mathbf{i} - 8\mathbf{j}$     (b)  $\mathbf{v} = -12\mathbf{i} + 9\mathbf{j}$     (c)  $\mathbf{v} = -4.5\mathbf{i} + 6\mathbf{j}$     (d)  $\mathbf{v} = 5\mathbf{i} + 5\mathbf{j}$   
 (e)  $\mathbf{v} = -4\mathbf{i} + 6\mathbf{j}$     (f)  $\mathbf{v} = 3\sqrt{2}\mathbf{i} - 5\sqrt{2}\mathbf{j}$     (g)  $\mathbf{v} = -4\sqrt{3}\mathbf{i} - 2\sqrt{3}\mathbf{j}$     (h)  $\mathbf{v} = -3\sqrt{5}\mathbf{i} + 6\sqrt{5}\mathbf{j}$

### Section 2

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1. Resistance experienced by engine =  $60000 \times 80 = 4800000$  ✓  
 Resistance experienced by truck =  $12000 \times 50 = 600000$  ✓  
 Train is travelling at constant speed, so acceleration is zero.



Considering whole system:  $X - 4800000 - 600000 = 0$  ✓

$X = 5400000$  ✓

The driving force of the engine = 5400 kN.

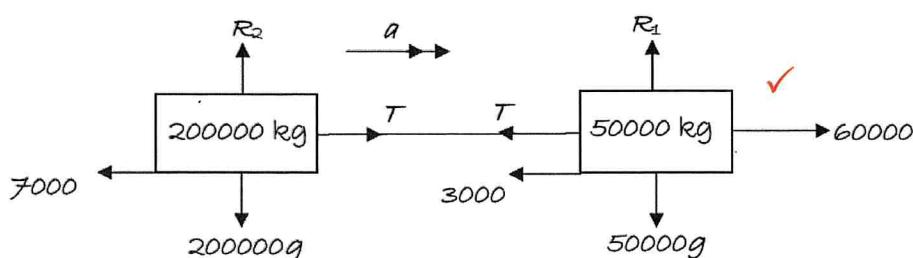
Considering truck:  $T - 600000 = 0$  ✓

$T = 600000$

The tension in the coupling = 600 kN. ✓

(7 marks)

2.



Considering the whole system:  $60000 - 3000 - 7000 = 250000a$  ✓

$50000 = 250000a$  ✓

$a = 0.2$

The acceleration of the system is  $0.2 \text{ ms}^{-2}$ . ✓

Considering the truck:  $T - 7000 = 200000 \times 0.2$  ✓

$$T - 7000 = 40000 \quad \checkmark$$

$$T = 47000$$

The tension in the coupling is 47000 N. ✓

(7 marks)

3. (i) Consider A, B and the pan as one particle;  $T - (0.8 + 0.3)g = (0.8 + 0.3) \times 1.5$  ✓

$$\Rightarrow T = 1.1g + 1.65 = 12.4 \text{ N} \quad (3 \text{ s.f.}) \quad \checkmark$$

(ii) Consider particle A only;  $R - 0.3g = 0.3 \times 1.5$  ✓

$$\Rightarrow R = 0.3g + 0.45 = 3.39 \text{ N} \quad \checkmark$$

(iii) Consider A and B as a single particle;  $R - 1.1g = 1.1 \times 1.5$  ✓

$$\Rightarrow R = 1.1g + 1.65 = 12.4 \text{ N} \quad (3 \text{ s.f.}) \quad \checkmark$$

(9 marks)

4.

(a) Car + trailer:  $2100a = 2380 - 280 - 630$

$$= 1470 \Rightarrow a = 0.7 \text{ m s}^{-2}$$

M1 A1

A1  
(3)

(b) e.g. trailer:  $700 \times 0.7 = T - 280$

$$\Rightarrow T = 770 \text{ N}$$

M1 A1 ✓

A1  
(3)

(c) Car:  $1400a' = 2380 - 630$

$$\Rightarrow a' = 1.25 \text{ m s}^{-2}$$

$$\text{distance} = 12 \times 4 + \frac{1}{2} \times 1.25 \times 4^2$$

$$= 58 \text{ m}$$

M1 A1

A1

↓ M1 A1 ✓

A1  
(6)

B1

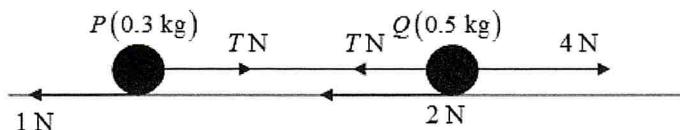
(1)  
13 marks

(d) Same acceleration for car and trailer

(Total 36 marks)

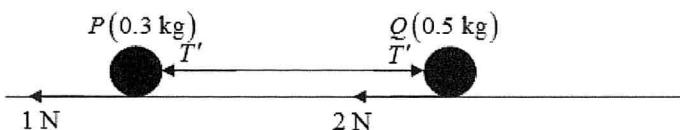
## Section 3

(a)	For system, $\uparrow$ , $T - 950g - 50g = 1000 \times -2$ $T = 7800 \text{ N}$	M1 A1 A1 <b>(3)</b>
(b)	For woman, $\uparrow$ , $R - 50g = 50 \times -2$ $R = 390 \text{ N}$	M1 A1 A1 <b>(3)</b> <b>[6]</b>



(a) For system N2L	$4 - 3 = 0.8a$ $a = 1.25 \text{ (m s}^{-2}\text{)}, 1.3$	M1 A1 A1 <b>(3)</b>
(b)	$v = u + at \Rightarrow v = 0 + 1.25 \times 6 = 7.5 \text{ (m s}^{-1}\text{)}$	M1 A1 <b>(2)</b>
(c) For P N2L	$T - 1 = 0.3 \times 1.25$ $T = 1.375 \text{ (N)}$ 1.38, 1.4	ft their $a$ M1 A1 ft A1 <b>(3)</b>

OR For Q N2L  $4 - 2 - T = 0.5 \times 1.25$



(d) For system N2L	$-3 = 0.8a \Rightarrow a = -3.75$ $v^2 = u^2 + 2as \Rightarrow 0^2 = 7.5^2 - 2 \times 3.75s$ $s = 7.5 \text{ (m)}$	M1 A1 M1 A1 <b>(4)</b>
(e) For P N2L	$T' + 1 = 0.3 \times 3.75$ $T' = 0.125 \text{ (N)}, 0.13$	M1 A1 A1 <b>(3)</b> <b>[15]</b>