

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel
Level 3 GCE**

Centre Number

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Candidate Number

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Mock Paper Set 1

(Time: 2 hours)

Paper Reference **9MA0/02**

Mathematics

Advanced

Paper 2: Pure Mathematics 2

You must have:

Mathematical Formulae and Statistical Tables, calculator

Total Marks

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Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 15 questions in this question paper. The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Question 3 continued

Lined area for writing the answer to Question 3.

(Total for Question 3 is 9 marks)

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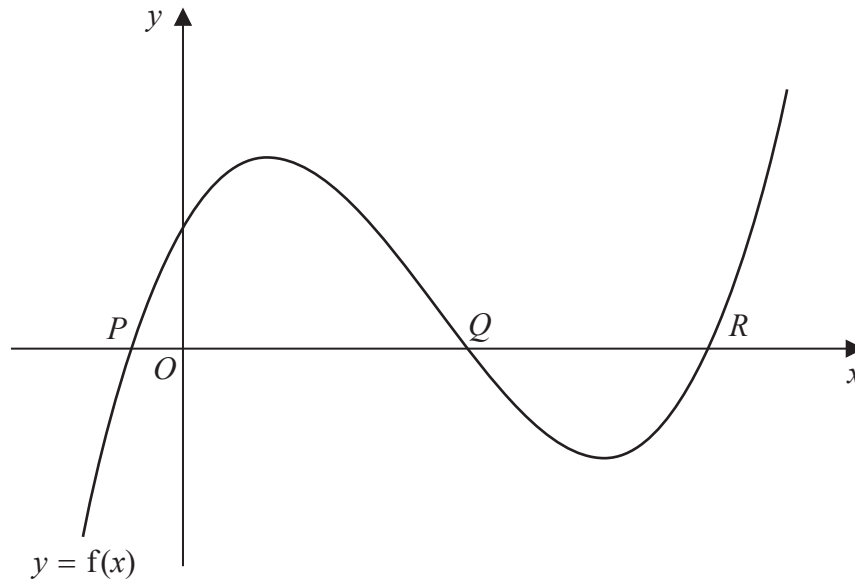


Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = f(x)$, where

$$f(x) = x^3 - 6x^2 + 7x + 2 \quad x \in \mathbb{R}$$

The curve cuts the x -axis at the points P , Q and R , as shown in Figure 1.

The coordinates of Q are $(2, 0)$

(a) Write $f(x)$ as a product of two algebraic factors. (2)

(b) Find, giving your answer in simplest form,
 (i) the exact x coordinate of P ,
 (ii) the exact x coordinate of R . (2)

(c) Deduce the number of real solutions, for $-\pi \leq \theta \leq 12\pi$, to the equation

$$\sin^3 \theta - 6 \sin^2 \theta + 7 \sin \theta + 2 = 0$$

 justifying your answer. (2)

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Question 4 continued

Lined area for writing the answer to Question 4.

(Total for Question 4 is 6 marks)

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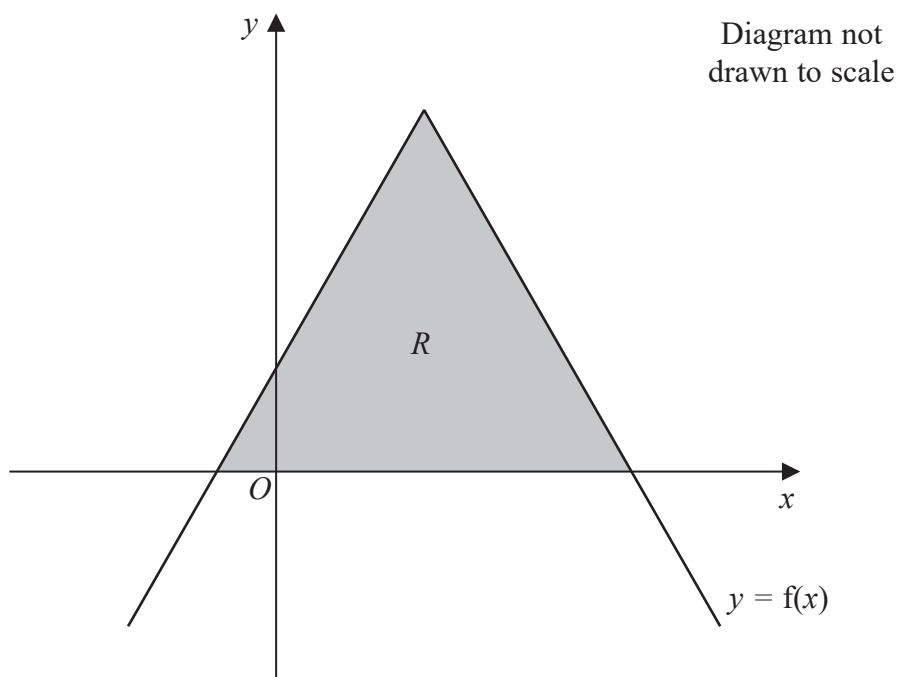


Figure 2

Figure 2 shows part of a graph with equation $y = f(x)$, where

$$f(x) = 7 - |3x - 5| \quad x \in \mathbb{R}$$

The finite region R , shown shaded in Figure 2, is bounded by the graph with equation $y = f(x)$ and the x -axis.

(a) Find the area of R , giving your answer in simplest form.

(4)

The equation

$$7 - |3x - 5| = k$$

where k is a constant, has two distinct real solutions.

(b) Write down the range of possible values for k .

(1)

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Question 5 continued

Lined writing area for the answer to Question 5.

(Total for Question 5 is 5 marks)



Question 6 continued

Lined area for writing the answer to Question 6. The area contains 25 horizontal lines.

(Total for Question 6 is 6 marks)

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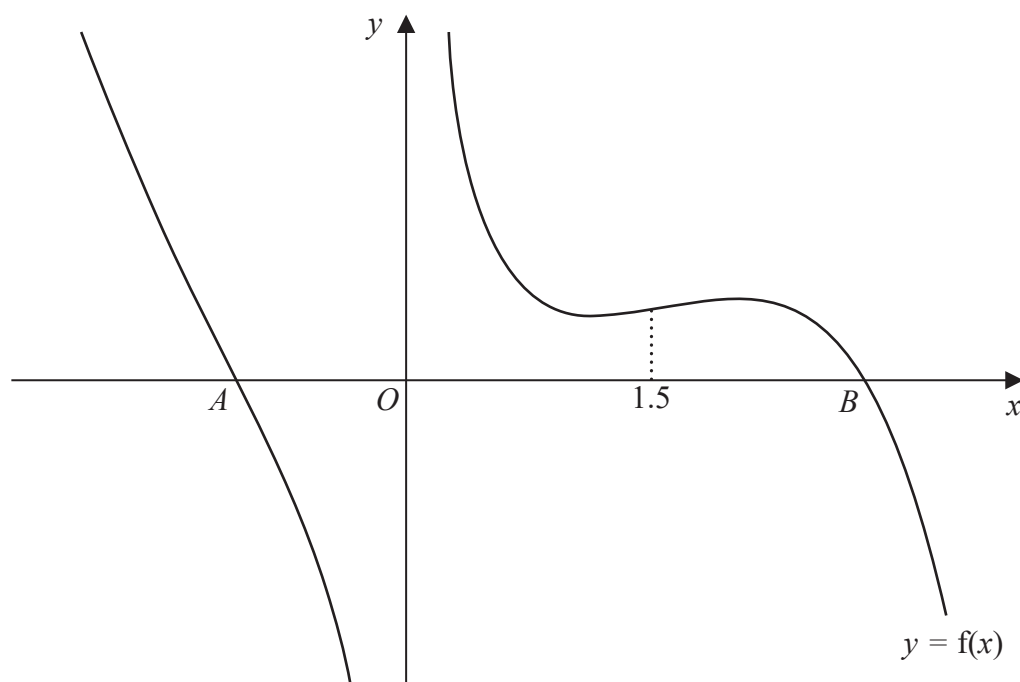


Figure 3

Figure 3 shows a plot of part of the curve with equation $y = f(x)$, where

$$f(x) = \frac{2}{x} - e^x + 2x^2 \quad x \in \mathbb{R}, x \neq 0$$

The curve cuts the x -axis at the point A , where $x = \alpha$, and at the point B , where $x = \beta$, as shown in Figure 3.

- (a) Show that α lies between -1.5 and -1 (2)
- (b) The iterative formula

$$x_{n+1} = -\sqrt{\left(\frac{1}{2}e^{x_n} - \frac{1}{x_n}\right)} \quad n \in \mathbb{N}$$

with $x_1 = -1$ can be used to estimate the value of α .

- (i) Find the value of x_3 to 4 decimal places.
- (ii) Find the value of α correct to 2 decimal places. (2)



9. The amount of antibiotic, y milligrams, in a patient's bloodstream, t hours after the antibiotic was first given, is modelled by the equation

$$y = ab^t$$

where a and b are constants.

- (a) Show that this equation can be written in the form

$$\log_{10} y = t \log_{10} b + c$$

expressing the constant c in terms of a .

(2)

A doctor measures the amount of antibiotic in the patient's bloodstream at regular intervals for the first 5 hours after the antibiotic was first given.

She plots a graph of $\log_{10} y$ against t and finds that the points on the graph lie close to a straight line passing through the point $(0, 2.23)$ with gradient -0.076

- (b) Estimate, to 2 significant figures, the value of a and the value of b .

(2)

With reference to this model,

- (c) (i) give a practical interpretation of the value of the constant a ,
(ii) give a practical interpretation of the value of the constant b .

(2)

- (d) Use the model to estimate the time taken, after the antibiotic was first given, for the amount of antibiotic in the patient's bloodstream to fall to 30 milligrams. Give your answer, in hours, correct to one decimal place.

(2)

- (e) Comment on the reliability of your estimate in part (d).

(1)

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Question 9 continued

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10. A biologist conducted an experiment to investigate the growth of mould on a slice of bread.

The biologist measured the surface area of bread, A cm², covered by mould at times, t days, after the start of the experiment.

Initially 9.00 cm² of the bread was covered by mould and 6 days later, 56.25 cm² of the bread was covered by mould.

In the biologist’s model, the rate of increase of the surface area of bread covered by mould, at any time t days, is proportional to the square root of that area.

By forming and solving a differential equation,

(a) show that the biologist’s model leads to the equation

$$A = \left(\frac{3}{4}t + 3 \right)^2 \qquad (6)$$

The biologist’s full set of results are shown in the table below.

t (days)	0	6	12	18	24	30
A (cm ²)	9.00	56.25	143.78	271.19	334.81	337.33

Table 1

Use the last four measurements from Table 1 to

(b) (i) evaluate the biologist’s model,

(ii) suggest a possible explanation of the results.

(3)

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Question 10 continued

Handwriting practice area with multiple horizontal lines.

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Question 10 continued

Lined writing area for the answer to Question 10.

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Question 10 continued

Lined writing area for the answer to Question 10.

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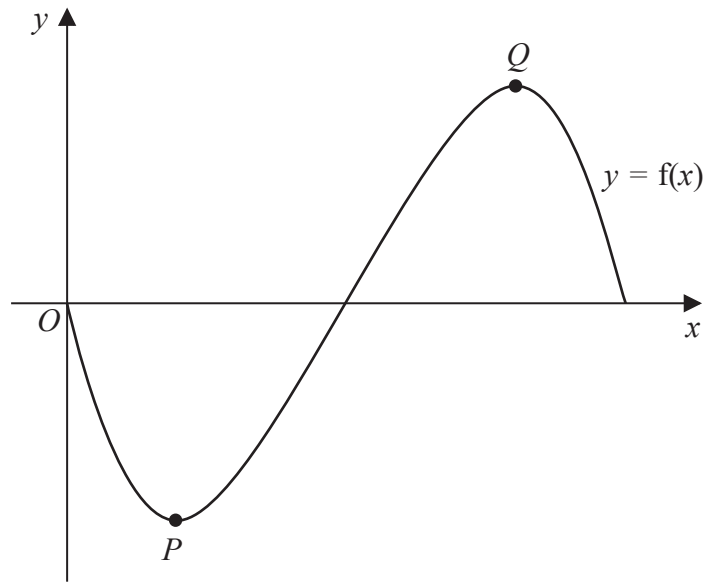


Figure 5

Figure 5 shows a sketch of the curve with equation $y = f(x)$, where

$$f(x) = \frac{\sin 2x}{-3 + \cos 2x} \quad 0 \leq x \leq \pi$$

The curve has a minimum turning point at P and a maximum turning point at Q , as shown in Figure 5.

(a) Show that the x coordinate of P and the x coordinate of Q are solutions of the equation

$$\cos 2x = \frac{1}{3} \tag{4}$$

(b) Hence find, to 2 decimal places, the x coordinate of the maximum turning point on the curve with equation

(i) $y = f(3x) + 5 \quad 0 \leq x \leq \frac{\pi}{3}$

(ii) $y = -f\left(\frac{1}{4}x\right) \quad 0 \leq x \leq 4\pi \tag{4}$

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Question 11 continued

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Question 11 continued

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Question 13 continued

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(Total for Question 13 is 7 marks)

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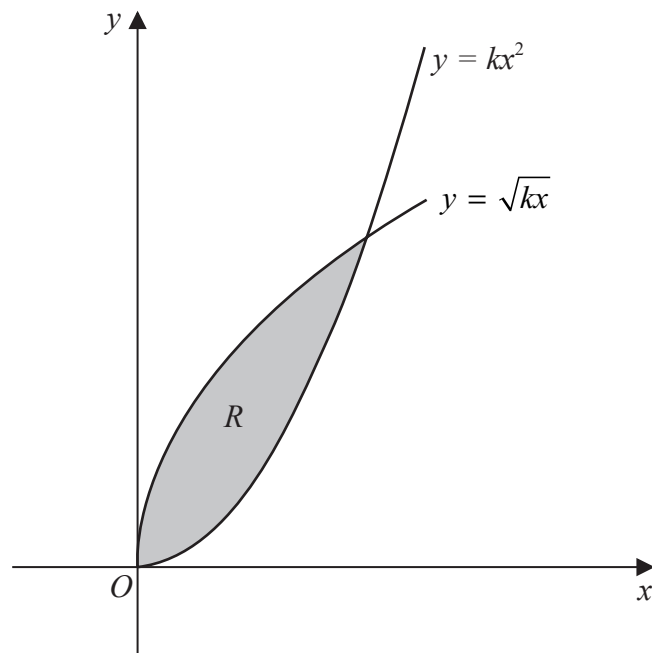


Figure 7

Figure 7 shows the curves with equations

$$y = kx^2 \quad x \geq 0$$

$$y = \sqrt{kx} \quad x \geq 0$$

where k is a positive constant.

The finite region R , shown shaded in Figure 7, is bounded by the two curves.

Show that, for all values of k , the area of R is $\frac{1}{3}$ (5)

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Question 14 continued

Lined writing area for the answer to Question 14.

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Question 15 continued

Lined writing area for the response to Question 15.

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Question 15 continued

Lined writing area for the answer to Question 15.

(Total for Question 15 is 7 marks)

TOTAL FOR PAPER IS 100 MARKS

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