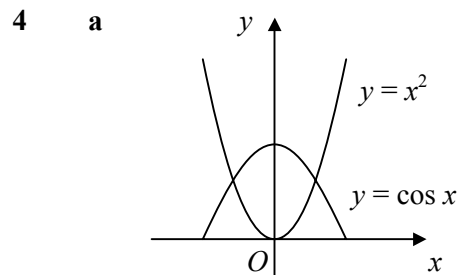


- 1 a let  $f(x) = x^3 - 7x - 11$   
 $f(3) = -5$   
 $f(4) = 25$   
 sign change,  $f(x)$  continuous  $\therefore$  root  
 b  $x_1 = 3.230712$   
 $x_2 = 3.225651$   
 $x_3 = 3.226479 = 3.23$  (2dp)

- 3 a  $f(0.4) = -0.809$   
 $f(0.5) = 0.307$   
 sign change,  $f(x)$  continuous  $\therefore$  root  
 $\therefore 0.4 < \alpha < 0.5$   
 b  $x_1 = 0.468857$   
 $x_2 = 0.463841$   
 $x_3 = 0.465157$   
 $x_4 = 0.464810$   
 $\therefore \alpha = 0.465$  (3dp)

- 5 a  $f(1.4) = 3.65$   
 $f(1.5) = -0.205$   
 sign change,  $f(x)$  continuous  $\therefore$  root  
 b  $e^{5-2x} - x^5 = 0 \Rightarrow x^5 = e^{5-2x}$   
 $\Rightarrow x = (e^{5-2x})^{\frac{1}{5}}$   
 $\Rightarrow x = e^{1-\frac{2}{5}x}, k = \frac{2}{5}$   
 c  $x_1 = 1.491825$   
 $x_2 = 1.496711$   
 $x_3 = 1.493789 = 1.494$  (3dp)

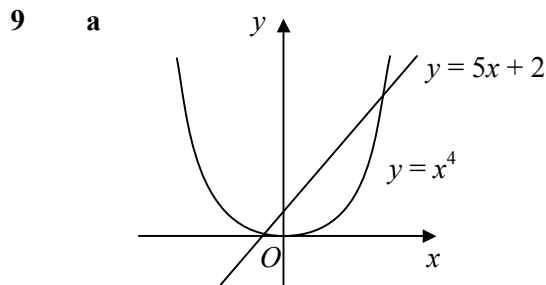
- 2 a  $f(4) = -2.29$  (3sf)  
 $f(5) = 0.829$  (3sf)  
 b sign change,  $f(x)$  continuous  $\therefore$  root  
 c  $4 \operatorname{cosec} x - 5 + 2x = 0$   
 $2x = 5 - 4 \operatorname{cosec} x$   
 $x = 2.5 - \frac{2}{\sin x}, a = 2.5, b = -2$   
 d  $x_1 = 4.545973$   
 $x_2 = 4.528018$   
 $x_3 = 4.534481 = 4.534$  (3dp)



- b  $\cos x - x^2 = 0 \Rightarrow \cos x = x^2$   
 the graphs  $y = \cos x$  and  $y = x^2$  intersect at 2 points, one for  $x < 0$  and one for  $x > 0$   
 $\therefore$  one negative and one positive real root  
 c let  $f(x) = \cos x - x^2$   
 $f(0.8) = 0.0567$   
 $f(0.9) = -0.188$   
 sign change,  $f(x)$  continuous  $\therefore$  root  
 d  $x_1 = 0.834690$   
 $x_2 = 0.819395$   
 $x_3 = 0.826235$   
 $x_4 = 0.823195$   
 $x_5 = 0.824550$   
 $\therefore$  root = 0.82 (2dp)

- 6 a  $f(1.3) = -0.341$   
 $f(1.4) = 0.383$   
 sign change,  $f(x)$  continuous  $\therefore$  root  
 b  $x_1 = 1.331571$   
 $x_2 = 1.354168$   
 $x_3 = 1.346907$   
 $x_4 = 1.349261$   
 c 1.35 (3sf)  
 d diverges leading to  $\ln$  of a -ve which is not real

- 7 **a**  $f'(x) = 6x^2 + 4$   
**b** for all real  $x$ ,  $x^2 \geq 0$   
 $\Rightarrow 6x^2 + 4 > 0$   
 $\therefore f(x)$  increasing for all  $x$   
 $\therefore y = f(x)$  only crosses  $x$ -axis once  
so exactly 1 real root  
**c**  $f(1.2) = -0.744$   
 $f(1.3) = 0.594$   
sign change,  $f(x)$  continuous  $\therefore$  root  
**d**  $x_1 = 1.280579$   
 $x_2 = 1.246945$   
 $x_3 = 1.261203$   
 $x_4 = 1.255199$   
 $\therefore$  root = 1.26 (2dp)  
**e**  $f(1.255) = -0.0267$   
 $f(1.265) = 0.109$   
sign change,  $f(x)$  continuous  $\therefore$  root
- 8 **a**  $3x + \ln x - x^2 = x \Rightarrow \ln x = x^2 - 2x$   
 $\Rightarrow x = e^{x^2 - 2x}$   
**b** let  $f(x) = 2x + \ln x - x^2$   
 $f(0.4) = -0.276$   
 $f(0.5) = 0.0569$   
sign change,  $f(x)$  continuous  $\therefore$  root  
**c**  $f(2.3) = 0.143$   
 $f(2.4) = -0.0845$   
sign change,  $f(x)$  continuous  $\therefore$  root  
**d**  $x_1 = 0.472367$   
 $x_2 = 0.485973$   
 $x_3 = 0.479134$   
 $x_4 = 0.482537$   
 $\therefore$   $x$ -coord of  $A = 0.48$  (2dp)  
**e**  $f(0.475) = -0.0201$   
 $f(0.485) = 0.0112$   
sign change,  $f(x)$  continuous  $\therefore$  root



- b**  $x^4 - 5x - 2 = 0 \Rightarrow x^4 = 5x + 2$   
the graphs  $y = x^4$  and  $y = 5x + 2$  intersect  
at 2 points, one for  $x < 0$  and one for  $x > 0$   
 $\therefore$  one negative and one positive real root  
**c**  $x_1 = 1.821160$   
 $x_2 = 1.825524$   
 $x_3 = 1.826420$   
 $x_4 = 1.826603 = 1.827$  (3dp)  
**d**  $x^4 - 5x - 2 = 0 \Rightarrow x^4 - 5x = 2$   
 $\Rightarrow x(x^3 - 5) = 2$   
 $\Rightarrow x = \frac{2}{x^3 - 5}$ ,  $a = 2$ ,  $b = -5$   
**e**  $x_1 = -0.394945$   
 $x_2 = -0.395132$   
 $x_3 = -0.395125$   
 $\therefore$  root =  $-0.3951$  (4dp)