

# SKILLS CHECK

QUESTION 1

Find the gradient of the curve  $y = \sqrt{x} + \frac{1}{x^2}$  at the point where  $x = 4$

QUESTION 2

$\mathbf{p} = 3\mathbf{i} + 2\mathbf{j}$   $\mathbf{q} = 2\mathbf{i} - 3\mathbf{j}$   
Find  $2\mathbf{p} - \mathbf{q}$

QUESTION 3

Write the expression  $\frac{1}{5}\log 32 - 2\log 4 + \log 64$  in the form  $\log x$

QUESTION 4

Solve  $3^{3x+1} = 6$  leaving your answer in exact form

QUESTION 5

Find  $\int 3x^2 - 2x + 4 \, dx$

WEEK 1

# SKILLS CHECK

QUESTION 1

$$y = \left(x + \frac{1}{x}\right)\left(\frac{1}{x^2} - x\right) \text{ find } \frac{dy}{dx}$$

QUESTION 2

$$p \begin{pmatrix} 4 \\ 3 \end{pmatrix} + q \begin{pmatrix} 1 \\ -2 \end{pmatrix} = \begin{pmatrix} -1 \\ -9 \end{pmatrix}$$

Find the values of p and q

QUESTION 3

What is the value of  $\log_4 64 + \log_3 27$  ?

QUESTION 4

Solve  $2^{3x-2} = 6$  leaving your answer in exact form

QUESTION 5

Find  $\int_1^2 6x^2 + 4x - 3 \, dx$

# SKILLS CHECK

QUESTION 1

Find coordinates of the stationary point of the curve  $y = \frac{4}{x^2} + x$

QUESTION 2

$a = -2i + 3j$   $b = 6i - j$   
Find  $|a - 2b|$

QUESTION 3

Write as a single log  
 $3\log x + 4\log y - 2\log(xy)$

QUESTION 4

M starts with a mass of 30g. The mass undissolved after  $t$  seconds is given by  $m = 30e^{-0.4t}$ . How long will it take for the mass to become half its original mass?  
(Answer correct to 3 s.f.)

QUESTION 5

Find  $\int_0^2 4x - 3x^2 + 1 \, dx$

# SKILLS CHECK

QUESTION 1

Find the coordinates of the point on the curve  $y = 2\sqrt{x} - 1$  where the gradient of the curve is 3

QUESTION 2

$$a \begin{pmatrix} 5 \\ 2 \end{pmatrix} - \begin{pmatrix} -2b \\ b \end{pmatrix} = \begin{pmatrix} 19 \\ 8 \end{pmatrix}$$

Find the values of a and b

QUESTION 3

$$\text{Solve } \log_3(4x + 1) = 2$$

QUESTION 4

The value of a car is depreciating. After  $t$  years it is worth (£V) is given by  $V = 15000e^{-0.3t}$ . After how many years will it be worth less than £5000 (3 s.f.)

QUESTION 5

$$\text{Find } \int_{-1}^1 2(x + 3)^2 dx$$

# SKILLS CHECK

QUESTION 1

Find the gradient(s) of the curve  $y = \frac{1}{x^2} - 4$  at the points where the curve intersects the x axis

QUESTION 2

Calculate the angle between  $\mathbf{a} = -2\mathbf{i} + 5\mathbf{j}$  and  $\mathbf{j}$

QUESTION 3

Solve  $2\log_a 4 - \log_a 4 + \frac{1}{2}\log_a 16 = \frac{1}{2}\log_a x$

QUESTION 4

The value, £V, of an investment of £4000 in a fixed rate scheme after  $t$  years is given by  $V = 4000 \times 1.035^t$ . Find the value of  $t$  when £V reaches £10000. Give your answer to 3 significant figures.

QUESTION 5

Find  $\int_1^2 3x^2 + 10x - 2 \, dx$

# SKILLS CHECK

QUESTION 1

Find the gradient of the curve  $y = \frac{x^2+2x}{\sqrt{x}}$  at the point where  $x = 9$

QUESTION 2

$\vec{OA} = \begin{pmatrix} 3 \\ 4 \end{pmatrix}$   $\vec{OB} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$ . Find  $\vec{CD}$  when  $\vec{CD} = 5\vec{AB}$

QUESTION 3

Solve  $2\log_2 x + \log_2 4 = 3$

QUESTION 4

The mass  $m$  of a radio active substance is given by the formula  $m = m_0 e^{-kt}$  when  $t$  is in seconds and  $m_0$  is the original mass. If the substance has a half life of 1 minute find the value of  $k$  (3 s.f.)

QUESTION 5

Find  $\int (4 - x)(3x + 2) dx$

WEEK 6

# SKILLS CHECK

QUESTION 1

Find the gradient of the tangent to the curve

$$y = \sqrt{x} \left( x^3 + \frac{1}{x^2} \right) \text{ at the point where } x = 4$$

QUESTION 2

$$p \begin{pmatrix} 2 \\ -1 \end{pmatrix} + q \begin{pmatrix} 5 \\ 2 \end{pmatrix} = \begin{pmatrix} 14 \\ 11 \end{pmatrix}$$

Find the values of p and q

QUESTION 3

$$\text{Solve } \log_a(x + 3) - \log_a 2 = \log_a 3x$$

QUESTION 4

200 ml of water is left in a glass. It evaporates and the volume left in the glass after t hours is given by  $V = 200e^{-kt}$ . If it takes 10 hours for 80 ml to evaporate find the value of k (3 s.f.)

QUESTION 5

$$\text{Find } \int x(x - 3)(2x + 1) dx$$