

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^5$  term in the expansion of  $\left(3 + \frac{1}{3}x\right)^9$

QUESTION 2

Prove that  $(\cos x - \sin x)^2 + (\sin x + \cos x)^2 = 2$

QUESTION 3

The graph of  $y = x^2 - \frac{1}{3}x^3 + ax$  passes through (3,24). Find the x- coordinates of the stationary points

QUESTION 4

$\mathbf{a} = 4\mathbf{i} - \mathbf{j}$  and  $\mathbf{b} = 3\mathbf{i} + 2\mathbf{j}$ . Find  $|2\mathbf{b} - \mathbf{a}|$

QUESTION 5

The graph of  $y = x^3$  is translated by vector  $\begin{bmatrix} -1 \\ 2 \end{bmatrix}$  find the equation of the resulting graph in the form  $y = x^3 + ax^2 + bx + c$

WEEK 1

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^4$  term in the expansion of  $(x - 1)(1 + 2x)^7$

QUESTION 2

Show that  $1 - \frac{\sin\theta\cos\theta}{\tan\theta} = \sin^2\theta$

QUESTION 3

If  $y = x(4 - x)$  calculate the finite area enclosed by the curve and the x - axis

QUESTION 4

If  $q = \begin{pmatrix} -3 \\ 4 \end{pmatrix}$  find the vector parallel to  $q$  with magnitude 25

QUESTION 5

The graph of  $y = x^2 - 2x$  is stretched by scale factor  $\frac{1}{2}$  parallel to the x-axis.  
Find the equation of the resulting graph

WEEK 2

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^5$  term in the expansion of  $\left(\frac{1}{3} - 3x\right)^{10}$

QUESTION 2

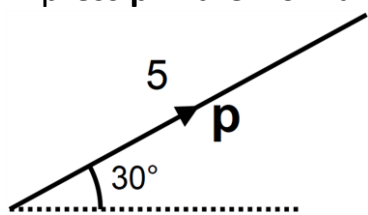
Show that  $\frac{\tan\theta\sin\theta}{1+\cos\theta} = \frac{1-\cos\theta}{\cos\theta}$

QUESTION 3

If  $y = x^3 - 5x^2 + kx$  has a stationary point where  $x = 2$ , find the  $y$  coordinate of this stationary point

QUESTION 4

Express  $\mathbf{p}$  in the form  $a\mathbf{i} + b\mathbf{j}$



QUESTION 5

The graph of  $y = x^3 + 2x^2 - x + 3$  is reflected in the  $y$ -axis.  
Find the equation of the resulting graph

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^4$  term in the expansion of  $(x^2 - 1)(2 - 3x)^5$

QUESTION 2

Show that  $\tan\theta + \frac{1}{\tan\theta} = \frac{1}{\sin\theta\cos\theta}$

QUESTION 3

Sketch the graph of  $y = x(x - 1)(x - 3)$ . Calculate the total area bounded by the graph of  $y$  and the  $x$  axis between  $x = 0$  and  $x = 3$

QUESTION 4

If  $\overrightarrow{OX} = 4i - 8j$  and  $\overrightarrow{OY} = -4i + 5j$  calculate  $|\overrightarrow{XY}|$

QUESTION 5

The point  $(-1, 2)$  lies on the graph of  $y = f(x)$ . State the coordinates of its image when the graph is transformed to  $y = 2f(x)$

WEEK 4

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^6$  term in the expansion of  $\left(\frac{1}{2} + 2x\right)^{12}$

QUESTION 2

Solve  $\frac{4\cos\theta - 1}{\tan\theta} = 2\sin\theta$   $0^\circ < \theta < 360^\circ$

QUESTION 3

Find the equation of the normal to the curve  $y = 8x^4 - 3$  at the point where  $x = -\frac{1}{2}$

QUESTION 4

$a\mathbf{i} + b\mathbf{j}$  is a vector of magnitude  $\sqrt{3}$  in the direction parallel to  $3\mathbf{i} - 3\mathbf{j}$   
Find the exact values of  $a$  and  $b$ .

QUESTION 5

The point  $(6, -10)$  lies on the graph of  $y = f(x)$ . State the coordinates of its image when the graph is transformed to  $y = f(2x)$

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^5$  term in the expansion of  $(x^2 - 2)(2 - 2x)^6$

QUESTION 2

Solve  $5\sin\theta = 1 + 2\cos^2\theta$   $0^\circ < \theta < 360^\circ$

QUESTION 3

Evaluate  $\int_{-3}^0 (2x + 3)^2 dx$

QUESTION 4

The position vector of A is  $6\mathbf{i} + 8\mathbf{j}$ . The position of the midpoint of the line joining A and B is  $3\mathbf{i} + 2\mathbf{j}$ . Find  $|\overrightarrow{AB}|$

QUESTION 5

The point  $(-1, 4)$  lies on the graph of  $y = f(x)$ . State the coordinates of its image when the graph is transformed to  $y = f(x-1) + 3$

WEEK 6

# SKILLS CHECK

QUESTION 1

Find the coefficient of the  $x^5$  term in the expansion of  $\left(3 - \frac{1}{3}x\right)^{11}$

QUESTION 2

Solve  $\sin(3x - 60^\circ) = 0.5$  for  $0^\circ \leq x \leq 360^\circ$

QUESTION 3

Find the equation of the tangent to the curve  $y = x^2\sqrt{x}$  at the point where  $x = 4$

QUESTION 4

O, A and B are vertices of a triangle. If  $\overrightarrow{OA} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}$  and  $\overrightarrow{OB} = \begin{pmatrix} 8 \\ 0 \end{pmatrix}$  calculate the area of the triangle

QUESTION 5

The point  $(-5, -2)$  lies on the graph of  $y = f(x)$ . State the coordinates of its image when the graph is transformed to  $y = f(x+5) + 2$