

AS SKILLS CHECKS

Half Term 5B (ANSWERS)		Week 1
1	$x(4-x) = 0 \quad x = 0 \quad x = 4$ $\int_0^4 4x - x^2 dx$ $= \left[2x^2 - \frac{1}{3}x^3 \right]$ $= \left[2 \times 4^2 - \frac{1}{3} \times 4^3 \right] - 0$ $= 10\frac{2}{3}$	
2	$\cos^2 x - 2\sin x \cos x + \sin^2 x + \cos^2 x + 2\sin x \cos x + \sin^2 x$ $= 2\cos^2 x + 2\sin^2 x$ $= 2(\cos^2 x + \sin^2 x)$ $= 2$	
3	$\log x^2 + \log \sqrt{y} - \log z^3$ $= \log \left(\frac{x^2 \sqrt{y}}{z^3} \right)$	
4	$x = 3 \quad y = 24 \quad 9 - \frac{1}{3} \times 27 + 3a = 24 \quad a = 8$ $\frac{dy}{dx} = 2x - x^2 + 8$ $\frac{dy}{dx} = 0 \quad 2x - x^2 + 8 = 0$ $x = -2 \quad x = 4$	
5	$9C5 \times 3^4 \times \left(\frac{1}{3}x\right)^5 = 42x^5$ <p><i>The coefficient = 42</i></p>	

Half Term 5B (ANSWERS)		Week 2
1	$\int_{-2}^8 16 + 6x - x^2 \, dx = \left[16x + 3x^2 - \frac{1}{3}x^3 + c \right]$ $\left[16 \times 8 + 3 \times 8^2 - \frac{1}{3} \times 8^3 \right] - \left[16 \times (-2) + 3 \times (-2)^2 - \frac{1}{3} \times (-2)^3 \right]$ $= 166\frac{2}{3}$	
2	$\cos^2 \theta - (1 - \cos^2 \theta) + 0.5 = 0$ $2\cos^2 \theta - 0.5 = 0$ $\cos \theta = \pm \frac{1}{2}$ $\theta = 60^\circ, 120^\circ, 240^\circ, 300^\circ$	
3	$\ln e^{-2x} + \ln e^x - \ln e^{2x}$ $= -2x + x - 2x$ $= -3x$	
4	$\frac{dy}{dx} = 3x^2 - 10x + k$ $3 \times 2^2 - 10 \times 2 + k = 0$ $k = 8$ $y = x^3 - 5x^2 + 8x$ $x = 2 \quad y = 4$	
5	$(1 + 2x)^7 = \dots + 7C3 \times 1^4 \times (2x)^3 + 7C4 \times 1^3 \times (2x)^4$ $= \dots 280x^3 + 560x^4 \dots$ $(x - 1)(1 + 2x)^7 = \dots 280x^4 - 560x^4$ $= -280x^4$	

Half Term 5B (ANSWERS)		Week 3
1	$y = x^3 - 4x^2 + 3x$ $\int_0^1 x^3 - 4x^2 + 3x \, dx$ $\int_1^3 x^3 - 4x^2 + 3x \, dx$ $\left[\frac{1}{4}x^4 - \frac{4}{3}x^3 + \frac{3}{2}x^2 + c \right]$ $= \frac{5}{12} - 2 \cdot \frac{2}{3}$ Total Area = $3\frac{1}{12}$	
2	$3 \frac{\sin \theta \sin \theta}{\cos \theta} = \cos \theta$ $3\sin^2 \theta - \cos^2 \theta = 0$ $3\sin^2 \theta - (1 - \sin^2 \theta) = 0$ $4\sin^2 \theta - 1 = 0$ $\sin \theta = \pm 0.5$ $\theta = 30^\circ, 150^\circ, 210^\circ, 330^\circ$	
3	$x = \frac{x+4}{x+1}$ $x^2 + x = x + 4$ $x^2 - 4 = 0$ $(x - 2)(x + 2) = 0$ $x = 2$ ($x = -2$ not possible)	
4	$6 = 2 - a + 10$ $a = 6$ $\frac{dy}{dx} = \frac{1}{\sqrt{x}} - 6$ $\frac{1}{\sqrt{x}} = 6$ $x = \frac{1}{36}$	
5	$10C5 \times \left(\frac{1}{3}\right)^5 \times (-3x)^5$ $= -252x^5$	

<p>1</p> $\int_4^9 3x + 4\sqrt{x} + 2 \, dx$ $\left[\frac{3}{2}x^2 + \frac{8}{3}x^{\frac{3}{2}} + 2x \right]$ $= \left[\frac{3}{2}9^2 + \frac{8}{3}9^{\frac{3}{2}} + 2 \times 9 \right] - \left[\frac{3}{2}4^2 + \frac{8}{3}4^{\frac{3}{2}} + 2 \times 4 \right] = 158\frac{1}{6}$
<p>2</p> $\frac{\sin\theta}{\cos\theta} + \frac{\cos\theta}{\sin\theta}$ $= \frac{\sin^2\theta + \cos^2\theta}{\cos\theta\sin\theta}$ $= \frac{1}{\sin\theta\cos\theta}$
<p>3</p> $(3x - 1)\ln 3 = \ln\left(\frac{1}{2}\right)$ $(3x - 1) = \frac{\ln\left(\frac{1}{2}\right)}{\ln 3}$ $x = \frac{1}{3}\left(\frac{\ln\left(\frac{1}{2}\right)}{\ln 3} + 1\right)$ $x = 0.123$
<p>4</p> $\frac{dy}{dx} = 32x^3$ $x = -0.5 \quad \text{Gradient of tangent} = -4$ $y = -2.5 \quad \text{Gradient of normal} = \frac{1}{4}$ $y + \frac{5}{2} = \frac{1}{4}(x + \frac{1}{2})$ $8y + 20 = 2x + 1$ $8y - 2x = -19$
<p>5</p> $5C4 \times (2)^1 \times (-3x)^4 = 810x^4$ $5C2 \times (2)^3 \times (-3x)^2 = 720x^2$ $\text{Coefficient of the } x^4 \text{ term} = 720 - 810$ $= -90$

1	$\int_1^9 1 + 2x + \sqrt{x} dx$ $\left[x + x^2 + \frac{2}{3}x^{\frac{3}{2}} \right]$ $= \left[9 + 9^2 + \frac{2}{3}9^{\frac{3}{2}} \right] - \left[1 + 1^2 + \frac{2}{3}1^{\frac{3}{2}} \right] = 105\frac{1}{3}$	
2	$4\cos\theta - 1 = 2\sin\theta\tan\theta$ $4\cos\theta - 1 = 2\frac{\sin^2\theta}{\cos\theta}$ $4\cos^2\theta - \cos\theta = 2(1 - \cos^2\theta)$ $6\cos^2\theta - \cos\theta - 2 = 0$ $\cos\theta = \frac{2}{3} \quad \cos\theta = -\frac{1}{2} \quad \theta = 48.2^\circ, 120^\circ, 240^\circ, 312^\circ$	
3	$0 + \log_a 6 + \log_a 64 - \log_a 4$ $= \log_a \left(\frac{6 \times 64}{4} \right)$ $= \log_a (96)$	
4	$\frac{dy}{dx} = \frac{5}{\sqrt{x}}$ $x = 4 \quad \text{Gradient of tangent} = \frac{5}{2}$ $\text{Gradient of normal} = -\frac{2}{5}$ $y = 10 \quad y - 10 = -\frac{2}{5}(x - 4) \quad 5y + 2x = 58$	
5	$12C6 \times \left(\frac{1}{2}\right)^6 \times (2x)^6 = 924x^6$	

1 $\int 4x^2 + 12x + 9 \, dx = \frac{4}{3}x^3 + 6x^2 + 9x + c$

$$\theta \dashv 9$$

$$= 9$$

2 $5\sin\theta = 1 + 2\cos^2\theta$
 $5\sin\theta = 1 + 2(1 - \sin^2\theta)$
 $2\sin^2\theta + 5\sin\theta - 3 = 0$
 $\sin\theta = \frac{1}{2}$ ($\sin\theta = -3$)

$$\theta = 30^\circ, 150^\circ$$

3 $e^{2x} = \frac{9}{4}$

$$2x = \ln\left(\frac{9}{4}\right)$$

$$x = \ln\left(\frac{3}{2}\right)$$

4 $y = x^{\frac{5}{2}}$ $\frac{dy}{dx} = \frac{5}{2}x^{\frac{3}{2}}$

$x = 4$ gradient of tangent = 20

$$y = 32$$

$$y - 32 = 20(x - 4)$$

$$y - 32 = 20x - 80 \quad 20x - y = 48$$

5 $6C5 \times (2)^1 \times (-2x)^5 = -382x^5$

$$6C3 \times (2)^3 \times (-2x)^3 = -1280x^3$$

Coefficient of the x^5 term = 768 - 1280

$$= -512$$

<p>1</p> $5x - x^2 = 10x - 2x^2$ $x^2 - 5x = 0 \quad x = 0 \text{ and } x = 5$ $\int_0^5 10x - 2x^2 - 5x + x^2 dx$ $\int_0^5 5x - x^2 dx = \left[\frac{5}{2}x^2 - \frac{1}{3}x^3 + c \right]$ $\frac{5}{2} \times 5^2 - \frac{1}{3} \times 5^3 = 20\frac{5}{6}$
<p>2</p> $3x - 60 = 30^\circ, 150^\circ, 390^\circ, 510^\circ, 750^\circ, 870^\circ$ $3x = 90^\circ, 210^\circ, 450^\circ, 570^\circ, 810^\circ, 930^\circ$ $x = 30^\circ, 70^\circ, 150^\circ, 190^\circ, 270^\circ, 310^\circ$
<p>3</p> $600e^{-0.5t} = 180$ $e^{-0.5t} = \frac{3}{10}$ $-0.5t = \ln\left(\frac{3}{10}\right)$ $t = -2\ln\left(\frac{3}{10}\right)$ $t = 2.41$
<p>4</p> $\frac{dy}{dx} = 5x^4 - 180x^2$ $5x^4 - 180x^2 = 0$ $5x^2(x^2 - 36) = 0$ $x = 0 \quad x = 6 \quad x = -6$
<p>5</p> $11C5 \times (3)^6 \times \left(-\frac{1}{3}x\right)^5 = -1386x^5$

