

**M1.** (i)  $v \left( = \frac{45}{152 \times 10^{-9}} \right) = 2.96 \times 10^8 \text{ m s}^{-1}$  **(1)**

2

(ii)  $t = 152 \text{ ns}$  **(1)**

$$t_0 \left[ = 152 \left( 1 - \frac{v^2}{c^2} \right)^{1/2} \right] = 152 \left( 1 - \left( \frac{2.96}{3.00} \right)^2 \right)^{1/2} \text{ (1)}$$

$= 25 \text{ ns}$  **(1)**

2  
QWC 2

[4]

- M2.** (a) (i) two beams (or rays) reach the observer **(1)**  
interference takes place between the two beams **(1)**  
bright fringe formed if/where (optical) path difference =  
whole number of wavelengths  
(or two beams in phase)  
[or dark fringe formed if/where (optical) path difference =  
whole number + 0.5 wavelengths]  
(or two beams out of phase by  $180^\circ$  /  $\pi/2$  /  $1/2$  cycle) **(1)**

- (ii) rotation by  $90^\circ$  realigns beams relative to direction of Earth's  
motion **(1)**  
no shift means no change in optical path difference between  
the two beams **(1)**  
( $\therefore$ ) time taken by light to travel to each mirror unchanged  
by rotation **(1)**  
distance to mirrors is unchanged by rotation **(1)**  
( $\therefore$ ) no shift means that the speed of light is unaffected  
[or disproves other theory] **(1)**

max 5

- (b) the speed of light does not depend on the motion of the  
light source **(1)** or that of the observer **(1)**

2

[7]

- M3.** (a) Newton's laws obeyed in an inertial frame  
[or inertial frames move at constant velocity relative to each other] **(1)**  
suitable example (e.g. object moving at constant velocity) **(1)**

2

(b) (i) (use of  $t = t_0 \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$  gives)  $t_0 = 18 \text{ (ns) (1)}$

$$t = 18 \times 10^{-9} \left(1 - \frac{(0.995c)^2}{c^2}\right)^{-1/2} \quad (1)$$

$$= 1.8 \times 10^{-7} \text{ s (1)}$$

(ii) time taken  $\left(= \frac{\text{distance}}{\text{speed}}\right) = \left(\frac{108}{0.995 \times 3.0 \times 10^8}\right) = 3.6 \times 10^{-7} \text{ s (1)}$

time taken = 2 half-lives, which is time to decrease to 25% intensity (1)

[alternative scheme: (use of  $l = l_0 \left(1 - \frac{v^2}{c^2}\right)^{1/2}$  gives)  $l_0 = 108 \text{ (m)}$

$$l = 108 \left(1 - \frac{(0.995c)^2}{c^2}\right)^{1/2} = 10.8 \text{ m (1)}$$

time taken  $\left(= \frac{10.8}{0.995c}\right) = 3.6 \times 10^{-8} \text{ s}$

= 2 half-lives, which is time to decrease to 25% intensity (1)]

5

[7]

**M4.** (i)  $E_k (= eV) (= 1.6 \times 10^{-19} \times 1.1 \times 10^9)$   
 $= 1.8 \times 10^{-10} \text{ (J) (1)}$  ( $1.76 \times 10^{-10} \text{ (J)}$ )

(ii) (use of  $E = mc^2$  gives)  $\Delta m = \left(\frac{1.8 \times 10^{-10}}{(3 \times 10^8)^2}\right) = 2.0 \times 10^{-27} \text{ (kg) (1)}$

$$= \frac{2.0 \times 10^{-27}}{1.67 \times 10^{-27}} m_0 = 1.2 m_0 \quad (1)$$

(allow C.E. for value of  $E_k$  from (i), but not 3rd mark)

$$\therefore m = m_0 + \Delta m \quad (1) \quad (= 2.2 m_0)$$

(iii) (use of  $m = m_0 \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$  gives)  $2.2m_0 = \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$  (1)

$$v = \left(1 - \frac{1}{2.2^2}\right)^{1/2} c \text{ (1)}$$

$$= 2.7 \times 10^8 \text{ m s}^{-1} \text{ (1)}$$

[7]

**M5.** (a) (i)  $t_0 = 800 \text{ (s) (1)}$

(use of  $t = t_0 \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$  gives)  $t = 800(1 - 0.994^2)^{-1/2}$  (1)  
 $= 7300 \text{ s (1)}$

(ii) distance ( $= 0.994ct = 0.994 \times 3 \times 10^8 \times 7300$ )  
 $= 2.2 \times 10^{12} \text{ m (1)}$  ( $2.18 \times 10^{12} \text{ m}$ )  
 (allow C.E. for value of  $t$  from (i))

4

(b) space twin's travel time = proper time (or  $t_0$ ) (1)

time on Earth,  $t = t_0 \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$  (1)  
 $t > t_0$

[or time for traveller slows down compared with Earth twin] (1)  
 space twin ages less than Earth twin (1)  
 travelling in non-inertial frame of reference (1)

max 3

[7]

**M6.** (a)  $10m_0 = m_0 \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$  (1)

gives  $\frac{v^2}{c^2} = 1 - 0.01 = 0.99$  (1)

$v (= 0.995c) = 2.98(5) \times 10^8 \text{ m s}^{-1}$  (1)

3

$$(b) \quad m = m_0 \left( 1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}} \quad (1)$$

$m \rightarrow \text{infinity as } v \rightarrow c \quad (1)$

[or  $m$  increases as  $v$  increases]

$$E_k (= mc^2 - m_0c^2) \rightarrow \text{infinity as } v \rightarrow c \quad (1)$$

$v = c$  would require infinite  $E_k$  (or mass) which is (physically)

impossible **(1)**

Max 3

[6]

**M7.** (i) time taken  $\left( \frac{\text{distance}}{\text{speed}} = \frac{34}{0.95 \times 3.0 \times 10^8} \right) = 1.1(9) \times 10^7 \text{ s} \quad (1)$

(ii) use of  $t = \frac{t_0}{(1 - v^2/c^2)^{1/2}}$  where  $t_0 = 18 \text{ ns}$

and  $t$  is the half-life in the detectors' frame of reference **(1)**

$$\therefore t = \frac{18 \times 10^{-9}}{(1 - 0.95^2)^{1/2}} = 57(.6) \times 10^{-9} \text{ s} \quad (1)$$

time taken for  $\pi$  meson to pass from one detector to the other  
= 2 half-lives (approx) (in the detectors' frame of reference) **(1)**

2 half-lives correspond to a reduction to 25%,  
so 75% of the  $\pi$  mesons passing the first detector  
do not reach the second detector **(1)**

**alternatives** for first 3 marks in (ii)

1. use of  $t = \frac{t_0}{\sqrt{1 - v^2/c^2}}$ , where  $t_0 = 18$  ns

$$= \frac{18}{(1 - 0.995^2)^{1/2}} = 57.6(\text{ns})$$

journey time in detector frame ( $= 2t$ ) =  $2 \times 57.6\text{ns}$  ( $\approx 2$  half-lives)

2. use of  $t = \frac{t_0}{\sqrt{1 - v^2/c^2}}$  where  $t = 119$  ns  
 = journey time in detector frame

$$t_0 = 119 \sqrt{1 - 0.995^2} = 37\text{ns}$$

journey time in rest frame =  $2 \times 18$  ns (2 half-lives)

[5]

**M8.** (a) (i) speed of light in free space independent of motion of source **(1)**

and of motion of observer **(1)**

(ii) laws of physics have the same form in all inertial frames **(1)**

inertial frame is one in which Newton's 1<sup>st</sup> law of motion is obeyed **(1)**

laws of physics unchanged in coordinate transformation **(1)**

from one inertial frame to another **(1)**

max 4

(b) (i)  $m (= m_0 (1 - v^2/c^2)^{-1/2}) = 1.9 \times 10^{-28} \times (1 - 0.995^2)^{-1/2}(\text{kg})$  **(1)**

$$= 1.9 \times 10^{-27} \text{ kg} \text{ (1)}$$

(ii)  $E (= mc^2) = 1.9 \times 10^{-27} \times (3.0 \times 10^8)^2$  **(1)**

$$= 1.7 \times 10^{10} \text{ J} \text{ (1)}$$

(iii)  $E_k (= E - m_0 c^2) = 1.7 \times 10^{10} (1.9 \times 10^{-28} \times (3.0 \times 10^8)^2)$  **(1)**

$$= 1.5 \times 10^{10} \text{ J} \text{ (1)}$$

6

[10]

**M9.** (a)  $c$  is the same, regardless of the speed of the light source or the observer **(1)**

1

(b) distance between detectors in rest frame of particles  
(=  $25 \times (1 - 0.98^2)^{1/2}$ ) = 5.0 m **(1)**

time taken in rest frame of particles  $\left( = \frac{\text{distance}}{\text{speed}} = \frac{5.0}{0.98c} \right) = 1.7 \times 10^{-8}$  s **(1)**

time taken to decrease by  $\frac{1}{4}$  = 2 half lives **(1)**

half life (=  $1.7 \times 10^{-8}/2$ ) =  $8.5 \times 10^{-9}$  s **(1)**

**[alternatively**

time taken in rest frame of detectors  $\left( = \frac{\text{distance}}{\text{speed}} = \frac{25.0}{0.98c} \right) = 8.5 \times 10^{-8}$  s  
time taken in rest frame of particles  
(=  $8.5 \times 10^{-8} \times (1 - 0.98^2)^{1/2}$ ) =  $1.7 \times 10^{-8}$  s)

4

**[5]**

**M10.** (a) (i)  $d_0$  = (speed  $\times$  time =  $1.8 \times 10^8 \times 95 \times 10^{-9}$ ) = 17(.1) m ✓

1

(ii)  $d$  (=  $d_0 (1 - v^2/c^2)^{1/2}$ )

$$= 17.1 \times (1 - (1.8 \times 10^8/3.0 \times 10^8)^2)^{1/2} \checkmark$$

$$= 14 \text{ m } \checkmark \text{ (or 13.7 m or 13.68 m)}$$

**or**

$$t = t_0 (1 - v^2/c^2)^{-1/2}$$

$$95 = t_0 (1 - (1.8 \times 10^8/3.0 \times 10^8)^2)^{-1/2} \text{ gives } t_0 = 76 \text{ ns } \checkmark$$

$$d = vt_0 = 1.8 \times 10^8 \times 76 \times 10^{-9} = 14 \text{ m } \checkmark \text{ (or 13.7 m or 13.68 m)}$$

2

(b)  $m (= m_0 (1 - v^2/c^2)^{-1/2})$   
 $= 1.67(3) \times 10^{-27} \times (1 - (1.8 \times 10^8/3.0 \times 10^8)^2)^{-1/2}$  ✓  
 $= 2.09 \times 10^{-27} \text{ kg}$  ✓

kinetic energy  $= (m - m_0) c^2$

or correct calculation of  $E = mc^2 (= 1.88 \times 10^{-10} \text{ J})$

or correct calculation of  $E_0 = m_0 c^2 (= 1.50 \times 10^{-10} \text{ J})$  ✓

$$\frac{\text{kinetic energy}}{\text{rest energy}} = \frac{(m - m_0)c^2}{m_0 c^2} = \frac{(2.09 - 1.67) \times 10^{-27}}{1.67 \times 10^{-27}}$$
 ✓

$= 0.25$  (allow 0.245 to 0.255 or  $\frac{1}{4}$  or 1:4) ✓

5

[8]

**M11.**

(a) bright (or dark) fringe is seen where the two beams are in phase (or out of phase by  $180^\circ$ ) ✓

changing the distance to either mirror changes the path (or phase) difference (between the two beams) so fringes shift ✓

2

(b) (i) speed of light was thought to depend on the speed of the light source (or the speed of the observer) ✓ (or on the motion of the Earth (through the aether))

distance travelled by each beam unchanged (by rotation) ✓

time difference between the two beams would change on rotation ✓

phase difference would therefore change (so fringes would shift) ✓

3

(ii) speed of light is independent of the speed (or motion) of the light source (or the observer) ✓

(or 'aether' hypothesis incorrect (owtte)) or absolute motion does not exist

1

[6]

M12. (a)

$$\text{(Using } m = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}} \text{ gives )}$$

$$2 = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \quad \text{or} \quad \sqrt{1 - \frac{v^2}{c^2}} = 0.5 \quad \checkmark$$

(Rearranging gives)

$$v (= \sqrt{1 - 0.5^2} c) = 0.866 c \text{ or } 2.6 \times 10^8 \text{ m s}^{-1} \quad \checkmark$$

Accept either answer.

2

- (b) curve starts at  $v=0$ ,  $m = m_0$  and rises smoothly  $\checkmark$

2nd mark; ecf from a if plotted correctly

curve passes through  $2m_0$  at  $v = 0.87 c$  ( $\pm 0.03c$  or in 2nd half of x-scale div containing  $0.87c$ )  $\checkmark$

3rd mark; There must be visible white space between the curve and the  $v = c$  line; also, the curve must reach  $7m_0$  at least.

curve is asymptotic at  $v = c$  ( and does not cross or touch  $v = c$  or curve back )  $\checkmark$

3

- (c) Energy =  $mc^2$  so (as  $v \rightarrow c$ ) energy of particle increases as mass increases  $\checkmark$

Alternative scheme for 1 mark only; mass infinite at  $v = c$  which is (physically) impossible  $\checkmark$

mass  $\rightarrow$  infinity as  $v \rightarrow c$  so energy  $\rightarrow$  infinity which is (physically) impossible  $\checkmark$

[OR for one mark only

force =  $ma$  so force increases as mass increases

Mass  $\rightarrow$  infinity as  $v \rightarrow c$  so force  $\rightarrow$  infinity which is (physically) impossible  $\checkmark$ ]

2

[7]



