

Pure 5 – Trig Equations and Proofs

Please <u>complete</u> this homework by ______. Start it early. If you can't do a question you will then have time to ask your teacher for help or go to a drop in session.

Section 1 – Review of previous topics. Please <u>complete</u> all questions.

1. Find the first 3 terms, in ascending powers of x, of the binomial expansion of

 $(2-3x)^5$,

giving each term in its simplest form.

2. (a) Find the first 3 terms, in ascending powers of x, of the binomial expansion of $(3 + bx)^5$

where *b* is a non-zero constant. Give each term in its simplest form. Given that, in this expansion, the coefficient of x^2 is twice the coefficient of *x*,

- (b) find the value of b.
- 3. (a) Find the first 4 terms of the binomial expansion, in ascending powers of x, of

$$\left(1+\frac{x}{4}\right)^8$$
,

giving each term in its simplest form.

(b) Use your expansion to estimate the value of $(1.025)^8$, giving your answer to 4 decimal places.

4. (a) Find the first 3 terms, in ascending powers of x, of the binomial expansion of $(2 - 9x)^4$,

giving each term in its simplest form.

 $f(x) = (1 + kx)(2 - 9x)^4$, where k is a constant. The expansion, in ascending powers of x, of f(x) up to and including the term in x^2 is $A - 232x + Bx^2$,

where A and B are constants.

(b) Write down the value of A.

(c) Find the value of k.

(d) Hence find the value of *B*.



Section 2 – Consolidation of this week's topic. Please <u>complete</u> all questions. (Total 58 marks)

- 1) Solve each equation for θ in the interval $0 \le \theta \le 2\pi$
 - a) $3sec^2\theta = 4tan^2\theta$ (4 marks)
 - b) $\cot^2\theta 3\csc \theta + 3 = 0$ (4 marks)
 - c) $sec^2\theta + 2tan\theta = 0$ (3 marks)
- 2) Solve each equation for *x* in the interval $-180^{\circ} \le x \le 180^{\circ}$
 - a) $tan^2x 2secx 2 = 0$ (5 marks)
 - b) $cosec^2x + 5cosecx + 2cot^2x = 0$ (5 marks)
 - c) $tan^2x + 4secx 2 = 0$ (4 marks)
- 3) Solve each equation in the interval $0 \le x \le 360^{\circ}$
 - a) $cot^2 2x + cosec 2x 1 = 0$ (6 marks)
 - b) $3cosec^2x 4sin^2x = 1$ (5 marks)
- 4) Prove each of the following identities

a)	$cosec^2x - sec^2x \equiv cot^2x - tan^2x$	(2 marks)
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- b) $(cosx 2secx)^2 \equiv cos^2 x + 4tan^2 x$ (3 marks)
- c) $(tanx + cotx)^2 \equiv sec^2x + cosec^2x$ (3 marks)
- d) $sec^2x + cosec^2x \equiv sec^2xcosec^2x$ (4 marks)

5)	a)	Given that $secx + tanx = -3$, use the identity $1 + tan^2x \equiv sec^2x$ to of $secx - tanx$.	o find the value (3 marks)
	b)	Deduce the values of:	· · · · ·
	,	(i) $secx$ (ii) $tanx$	(3 marks)
	C)	Hence solve, in the interval $-180^{\circ} \le x \le 180^{\circ}$, $secx + tanx = -3$	(3 marks)