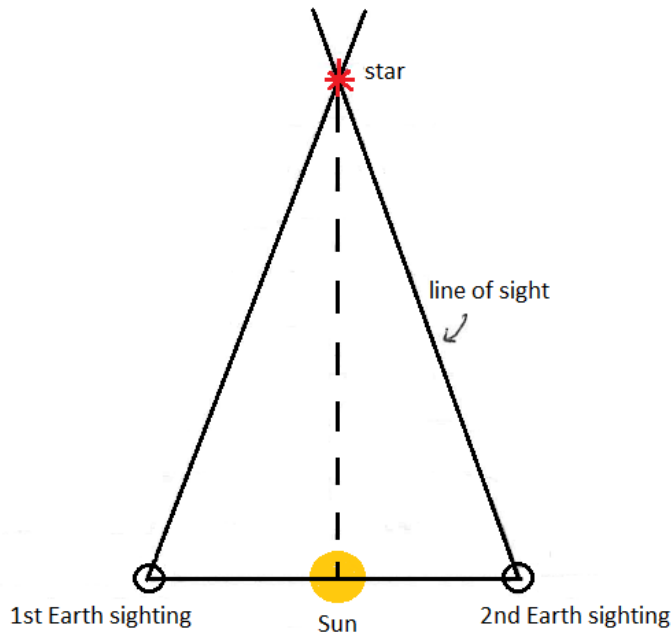


ASTROPHYSICS

2-1 Star magnitudes

1.



The line of sight to a nearby star changes as the Earth moves round in its orbit. It appears to change position against the fixed background of more distant stars as a result.

2. (a) The absolute magnitude of a star is defined as the star's apparent magnitude if it was at a distance of 10 parsecs from Earth.

(b) (i) angular shift = 0.45 arc seconds so $\theta = \frac{0.45}{2}$ arc seconds

$$\begin{aligned}
 d \text{ (in parsecs)} &= \frac{1}{\theta \text{ (in arc seconds)}} \\
 &= \frac{2}{0.45} \\
 &= 4.444\dots \text{ parsecs} \\
 &= 4.4 \text{ pc to 2 sf}
 \end{aligned}$$

(ii) apparent magnitude, $m = +9.8$

$$m - M = 5 \log \left(\frac{d}{10} \right)$$

$$+9.8 - M = 5 \log \left(\frac{4.4}{10} \right)$$

$$M = 9.8 - (-1.78) = +11.582\dots = +11.6 \text{ to 3 sf}$$

3. (a) (i) $m = +3.0$, $d = 100$ pc

$$m - M = 5 \log \left(\frac{d}{10} \right)$$

$$\begin{aligned} M &= m - 5 \log \left(\frac{d}{10} \right) \\ &= +3.0 - 5 \log \left(\frac{100}{10} \right) \\ &= +3.0 - 5.0 \\ &= -2.0 \text{ to 2 sf} \end{aligned}$$

(ii) $m = -1.4$, $d = 2.7$ pc

$$m - M = 5 \log \left(\frac{d}{10} \right)$$

$$\begin{aligned} M &= m - 5 \log \left(\frac{d}{10} \right) \\ &= -1.4 - 5 \log \left(\frac{2.7}{10} \right) \\ &= -1.4 - (-2.8) \\ &= +1.4 \text{ to 2 sf} \end{aligned}$$

(b) $M = +3.5$, $d = 30$ pc

$$M = m - 5 \log \left(\frac{d}{10} \right)$$

$$\begin{aligned} m &= M + 5 \log \left(\frac{d}{10} \right) \\ &= +3.5 + 5 \log \left(\frac{30}{10} \right) \\ &= +3.5 + 2.4 \\ &= +5.9 \text{ to 2 sf} \end{aligned}$$

4. (a) $m = -26.8$, $d = \frac{1}{206\,000}$ pc (1 AU)

$$m - M = 5 \log \left(\frac{d}{10} \right)$$

$$\begin{aligned} M &= m - 5 \log \left(\frac{d}{10} \right) \\ &= -26.8 - 5 \log \left(\frac{1}{206\,000 \times 10} \right) \\ &= -26.8 - (-31.6) \\ &= +4.8 \text{ to 2 sf} \end{aligned}$$

$$(b) M = +4.8, d = 5.2 \text{ AU} = \frac{5.2}{206\,000} \text{ pc} \quad (2.52 \times 10^{-5} \text{ pc})$$

$$M = m - 5 \log \left(\frac{d}{10} \right)$$

$$m = M + 5 \log \left(\frac{d}{10} \right)$$

$$= +4.8 + 5 \log \left(\frac{30}{10} \right)$$

$$= +4.8 + (-28.0)$$

$$= -23.2 \quad \text{to 2 sf}$$