

MEDICAL PHYSICS

5-2 X-rays and matter

1. (a) The half-value thickness (HVT) of a substance is the thickness required to reduce the intensity of the X-rays to 50%.

(b) (i) HVT = 15 mm for 50 keV X-rays.

$$\begin{aligned}x_{1/2} &= \frac{\ln 2}{\mu} \text{ therefore } \mu = \frac{\ln 2}{x_{1/2}} = \frac{\ln 2}{15 \times 10^{-3}} \\ &= 46.2\dots \\ &= 46 \text{ m}^{-1}\end{aligned}$$

(ii) $I = I_0 e^{-\mu x}$ therefore $\frac{I}{I_0} = e^{-\mu x}$

$$\begin{aligned}\frac{I}{I_0} &= e^{-(46 \times 10 \times 10^{-3})} = e^{-0.46} \\ &= 0.63\end{aligned}$$

Therefore 63% of the intensity remains and the reduction is 37%

2. 80 keV, $I_0 = 1.4 \times 10^{-2} \text{ Wm}^{-2}$, $x = 0.50 \text{ mm} = 5.0 \times 10^{-4} \text{ m}$, $\mu = 690 \text{ m}^{-1}$

$$\begin{aligned}\text{(a) (i) } I &= I_0 e^{-\mu x} = 1.4 \times 10^{-2} \times e^{-(690 \times 5.0 \times 10^{-4})} \\ &= 1.4 \times 10^{-2} \times e^{-0.345} \\ &= 9.9 \times 10^{-3} \text{ Wm}^{-2}\end{aligned}$$

$$\begin{aligned}\text{(ii) therefore energy absorbed} &= (1.4 \times 10^{-2} - 9.9 \times 10^{-3}) \text{ Wm}^{-2} \\ &= 4.1 \times 10^{-3} \text{ Wm}^{-2}\end{aligned}$$

Area of the sheet = $0.10 \times 0.10 = 1.0 \times 10^{-2} \text{ m}^2$

$$\begin{aligned}\text{Therefore, energy absorbed per second by the sheet} &= 4.1 \times 10^{-3} \text{ Wm}^{-2} \times 1.0 \times 10^{-2} \text{ m}^2 \\ &= 4.1 \times 10^{-5} \text{ W or Js}^{-1}\end{aligned}$$

$$\text{(b) } \frac{I}{I_0} = e^{-0.46} = 0.25 = e^{-(690 \times x)}$$

$$-690x = \ln(0.25)$$

$$x = \frac{\ln 0.25}{-690}$$

$$= 2.0 \times 10^{-3} \text{ m or 2 mm}$$

3. $\mu_m = 0.012 \text{ m}^2\text{kg}^{-1}$, $\rho = 2700 \text{ kgm}^{-3}$

(a) The mass attenuation coefficient is defined by the equation

$$\mu_m = \frac{\mu}{\rho}$$

where μ is the attenuation coefficient and
 ρ is the density of the material

$$\begin{aligned} \text{(b)} \quad \mu &= \rho\mu_m = 2700 \text{ kgm}^{-3} \times 0.012 \text{ m}^2\text{kg}^{-1} \\ &= 32.4 \text{ m}^{-1} \end{aligned}$$

$$x_{1/2} = \frac{\ln 2}{\mu} = \frac{\ln 2}{32.4}$$

$$= 0.0213\dots$$

$$= 0.021 \text{ m to 2 sf} \quad \text{or } 21 \text{ mm}$$

4. (a) (i) A metal filter is placed in the path of the X-ray beam in order to remove photons with an energy of less than about 30 keV which are absorbed by soft tissue as well as bone.

(ii) A suitable metal for such a filter would be copper, tin or lead.

(b) X-ray photons with an energy greater than about 100 keV are not used for X-ray imaging because all tissue types absorb them fairly equally so there would be no contrast between different types of tissue.