

GCSE Mathematics

Practice Tests: Set 4

Paper 1H (Non-calculator)

Time: 1 hour 30 minutes

You should have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator.

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- **Calculators may be used.**
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must **show all your working out.**



Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1. Write these numbers in order of size.
Start with the smallest number.

$$2^5 \quad 64^{\frac{1}{2}} \quad 4^3 \quad 8^{\frac{1}{3}} \quad 16 \quad 64^0$$

You must show clearly how you got your answer.

$$32 \quad 8 \quad 64 \quad 2 \quad 16 \quad 1$$

$$64^0 \quad 8^{\frac{1}{3}} \quad 64^{\frac{1}{2}} \quad 16 \quad 2^5 \quad 4^3$$

(Total 3 marks)

2. There are 50 counters in a bag.

The counters are blue or yellow or black or white.
A counter is taken at random from the bag.

The table shows each of the probabilities that the counter will be blue or black or white.

Colour	blue	yellow	black	white
Probability	0.4		0.3	0.16

Work out the number of yellow counters in the bag.

$$0.4 + 0.3 + 0.16 = 0.86$$

$$1 - 0.86 = 0.14$$

$$0.14 \times 50 = 7$$

.....7.....

(Total 4 marks)

3. Buses to Acton leave a bus station every 24 minutes.
Buses to Barton leave the same bus station every 20 minutes.

A bus to Acton and a bus to Barton both leave the bus station at 9 00 a.m.

When will a bus to Acton and a bus to Barton next leave the bus station at the same time?

24, 48, 72, 96, 120

20, 40, 60, 80, 100, 120

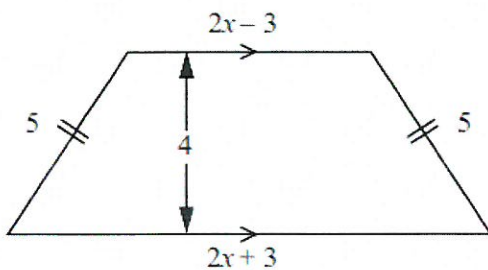
120 mins = 2 hrs

9 + 2 = 11

..... 11 am

(Total 3 marks)

4. Here is a trapezium.



All the measurements are in cm.
The area of the trapezium is 18 cm^2 .

Calculate the numerical value of the perimeter of the trapezium.

$$\begin{aligned} \text{AREA} &= \frac{4}{2} (2x - 3 + 2x + 3) \\ &= 2(4x) \\ &= 8x \end{aligned}$$

$$\therefore 8x = 18$$

$$\therefore x = \frac{18}{8} = \frac{9}{4} = 2\frac{1}{4} = 2.25$$

$$\begin{aligned} \text{PERIMETER} &= (2 \times 2.25 - 3) + (2 \times 2.25 + 3) \\ &\quad + 5 + 5 \\ &= 4.5 - 3 + 4.5 + 3 + 10 \\ &= \cancel{20} 19 \end{aligned}$$

..... ~~20~~ 19cm

(Total 6 marks)

5. The normal price of a television is reduced by 30% in a sale.

The sale price of the television is £350

Work out the normal price of the television.

$$\text{SALE PRICE} = 70\% \text{ OF NORMAL PRICE}$$

$$350 = 0.7 \times \text{NORMAL PRICE}$$

$$\text{NORMAL PRICE} = \frac{350}{0.7} = \frac{3500}{7} = 500$$

£500.....

(Total 3 marks)

6. Work out an estimate for the value of

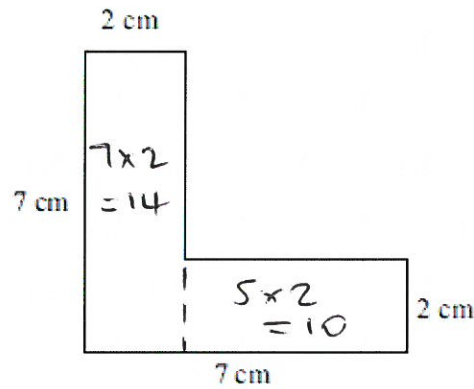
$$\frac{6.8 \times 191}{0.051} \approx \frac{7 \times 200}{0.05} = \frac{1400}{0.05}$$

$$= 1400 \times 20$$

.....
28000

(Total 3 marks)

7.



The diagram shows the cross-section of a solid prism.

The length of the prism is 2 m. = 200 cm

The prism is made from metal.

The density of the metal is 8 grams per cm^3 .

Work out the mass of the prism.

$$\text{AREA OF CROSS-SECTION} = 14 + 10 = 24 \text{ cm}^2$$

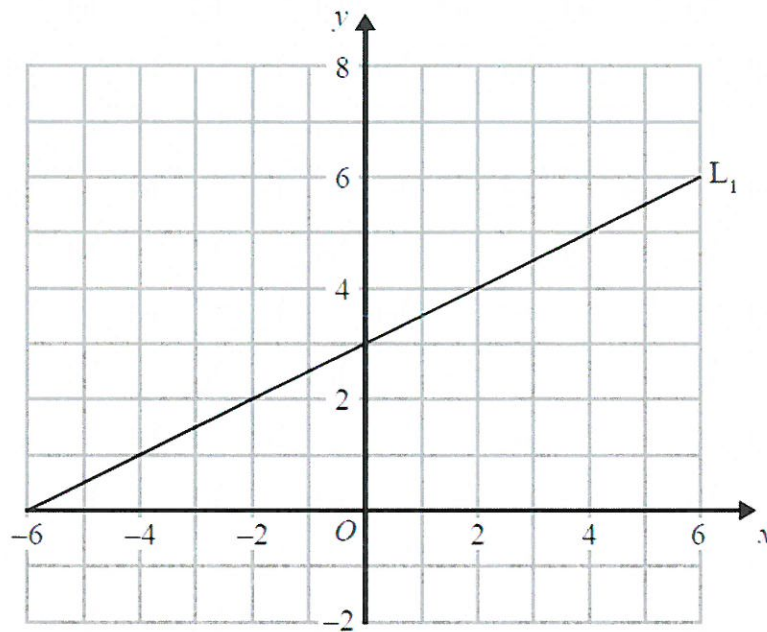
$$\text{VOLUME OF PRISM} = 24 \times 200 = 4800 \text{ cm}^3$$

$$\begin{aligned} \text{MASS} &= 4800 \times 8 \\ &= 38400 \end{aligned}$$

38400g

(Total 5 marks)

8. The diagram shows a straight line, L_1 , drawn on a grid.



A straight line, L_2 , is parallel to the straight line L_1 and passes through the point $(0, -5)$.

Find an equation of the straight line L_2 .

$$\text{GRADIENT OF } L_2 = \text{GRADIENT OF } L_1 = \frac{3}{6} = \frac{1}{2}$$

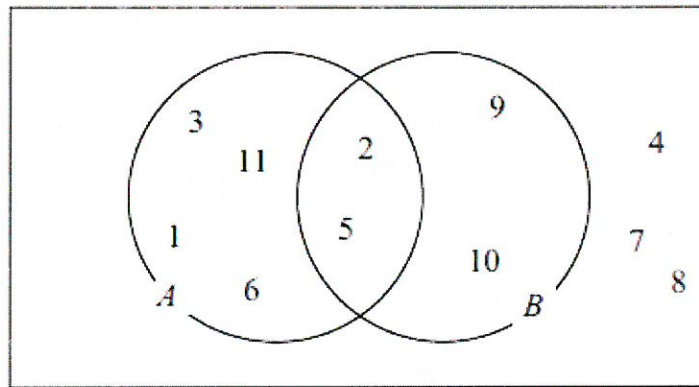
$$\text{EQUATION OF } L_2 = y = \frac{1}{2}x + c$$

$$\therefore -5 = \frac{1}{2} \times 0 + c \quad \therefore c = -5$$

$$y = \frac{1}{2}x - 5$$

(Total 3 marks)

9. The Venn diagram shows the numbers 1 to 11



- (a) Work out $P(A \cup B)$

$$\frac{8}{11}$$

..... (2)

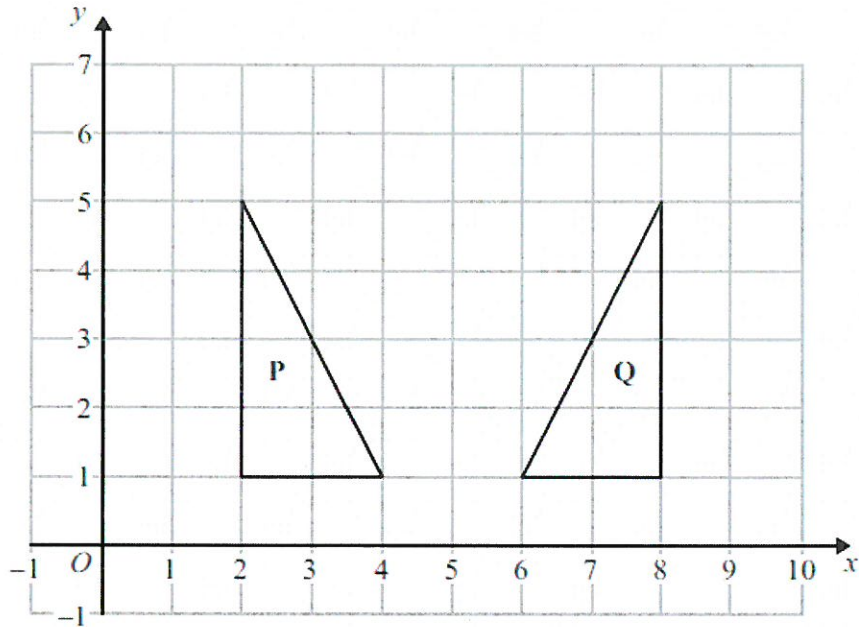
- (b) Work out $P(B')$

$$\frac{7}{11}$$

..... (2)

(Total 4 marks)

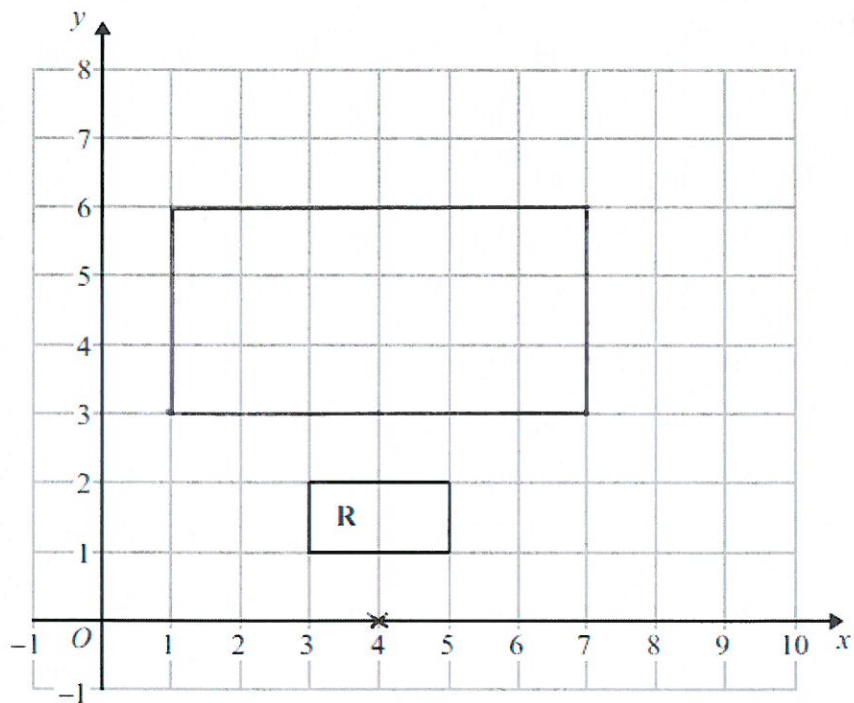
10.



(a) Describe fully the single transformation that maps triangle **P** onto triangle **Q**.

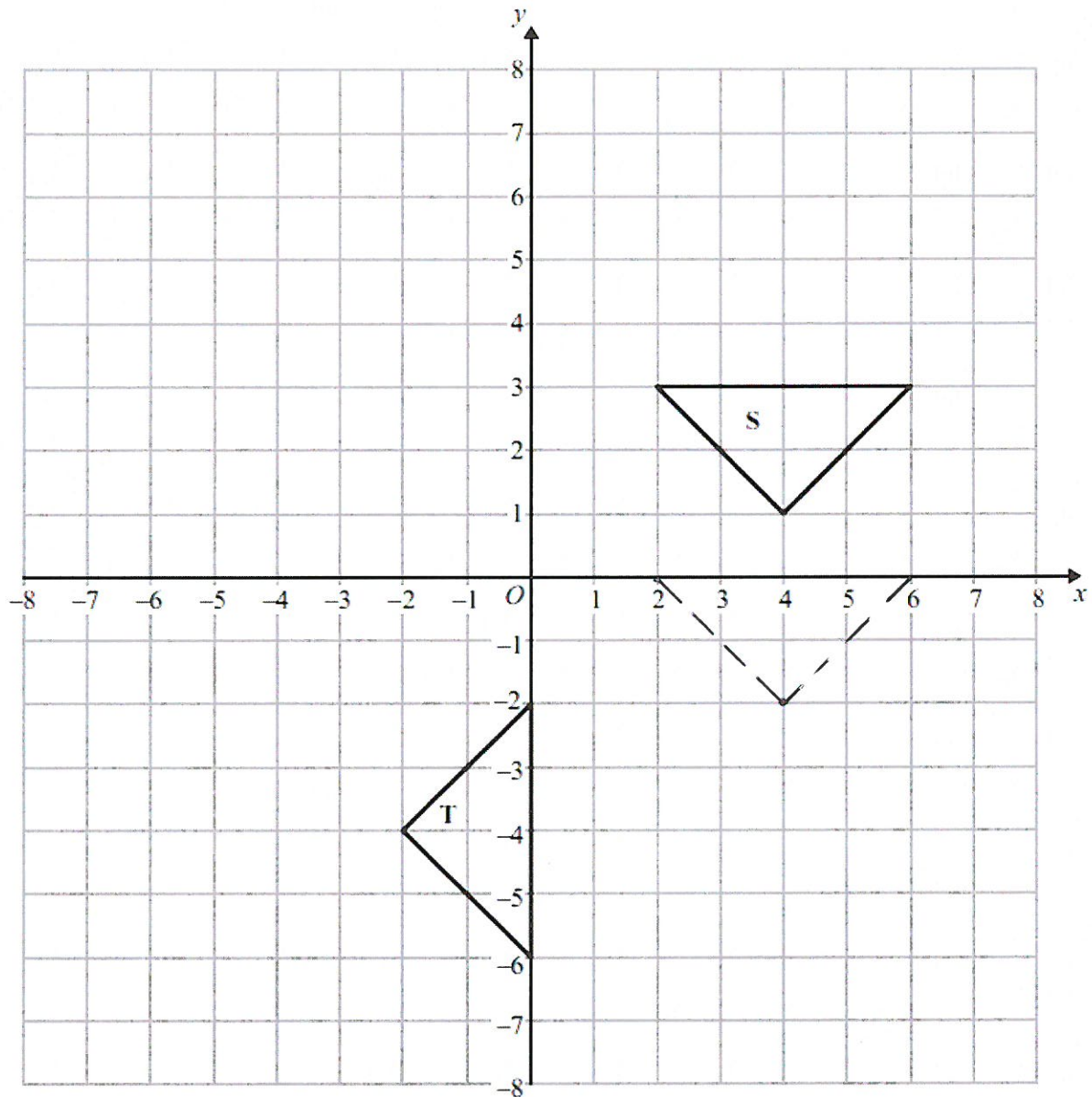
REFLECTION IN $x = 5$

(2)



(b) Enlarge rectangle **R**, with scale factor 3 and centre (4, 0).

(2)



Shape S can be transformed to shape T by the translation $\begin{pmatrix} 0 \\ -3 \end{pmatrix}$ followed by a rotation.

(c) Describe the rotation.

..... ROTATION 90° COUNTERCLOCKWISE ABOUT $(0, 0)$

.....

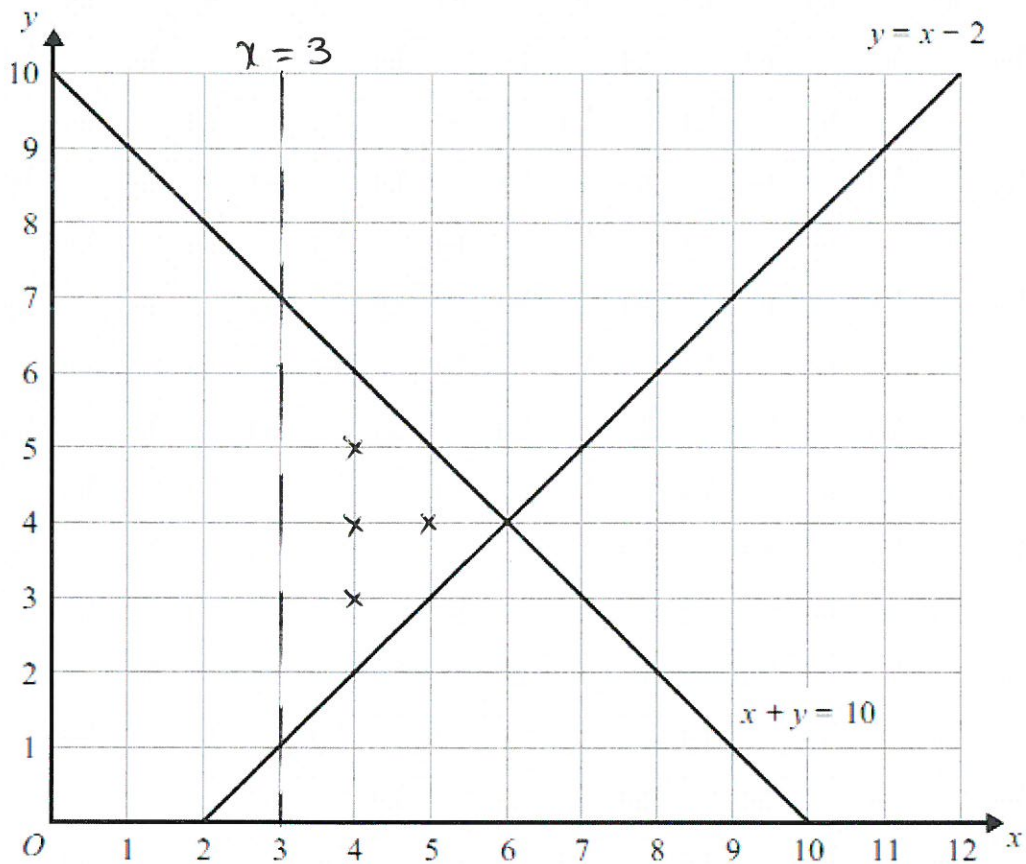
.....

.....

(3)

(Total 7 marks)

11. The lines $y = x - 2$ and $x + y = 10$ are drawn on the grid.



On the grid, mark with a cross (\times) each of the points with integer coordinates that are in the region defined by

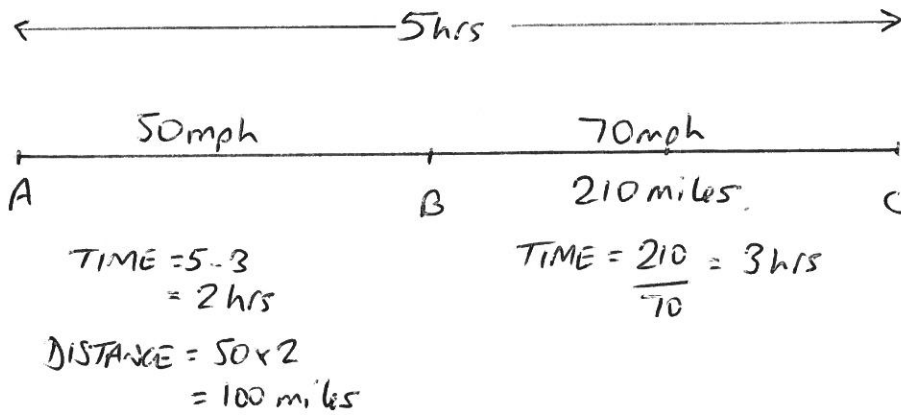
$$\begin{aligned}y &> x - 2 \\x + y &< 10 \\x &> 3\end{aligned}$$

(Total 3 marks)

12. Harry travels from Appleton to Brockley at an average speed of 50 mph.
He then travels from Brockley to Cantham at an average speed of 70 mph.

Harry takes a total time of 5 hours to travel from Appleton to Cantham.
The distance from Brockley to Cantham is 210 miles.

Calculate Harry's average speed for the total distance travelled from Appleton to Cantham.



$$\text{TOTAL DISTANCE} = 100 + 210 = 310 \text{ miles}$$

$$\text{SPEED} = \frac{310}{5} = 62 \text{ mph.}$$

..... 62 mph

(Total 4 marks)

13.

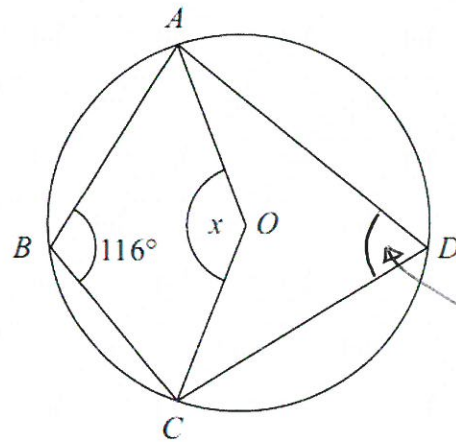


Diagram NOT
accurately drawn

OPPOSITE ANGLES IN A CYCLIC
QUADRILATERAL ADD UP TO 180
 $\therefore \hat{CDA} = 180 - 116 = 64^\circ$

A, B, C and D are points on the circumference of a circle with centre O .
Angle $ABC = 116^\circ$.

Find the size of the angle marked x .
Give reasons for your answer.

ANGLE AT CENTRE = 2 x ANGLE AT CIRCUMFERENCE

$$\therefore x = 2 \times 64 = 128$$

$$x = 128^\circ$$

(Total 4 marks)

14. The n th term of a quadratic sequence is $n^2 + 3n - 2$

(a) Find the fourth term of this sequence.

$$n = 4$$

$$\begin{aligned} & 4^2 + 3 \times 4 - 2 \\ & = 16 + 12 - 2 \end{aligned}$$

$$\dots\dots\dots 26 \dots\dots\dots (2)$$

Here are the first five terms of a different quadratic sequence.

1 7 17 31 49

(b) Find, in terms of n , an expression for the n th term of this sequence.

$$\begin{array}{cccccc} & +6 & & +10 & & +14 & & +18 \\ & & +4 & & +4 & & +4 & \end{array}$$

$$T_n = an^2 + bn + c \quad a = \frac{1}{2} \times 4 = 2$$

$$\therefore T_n - 2n^2 = bn + c$$

T_n	1	7	17	31	49
$T_n - 2n^2$	-1	-1	-1	-1	-1

$$\therefore b = 0 \quad c = -1$$

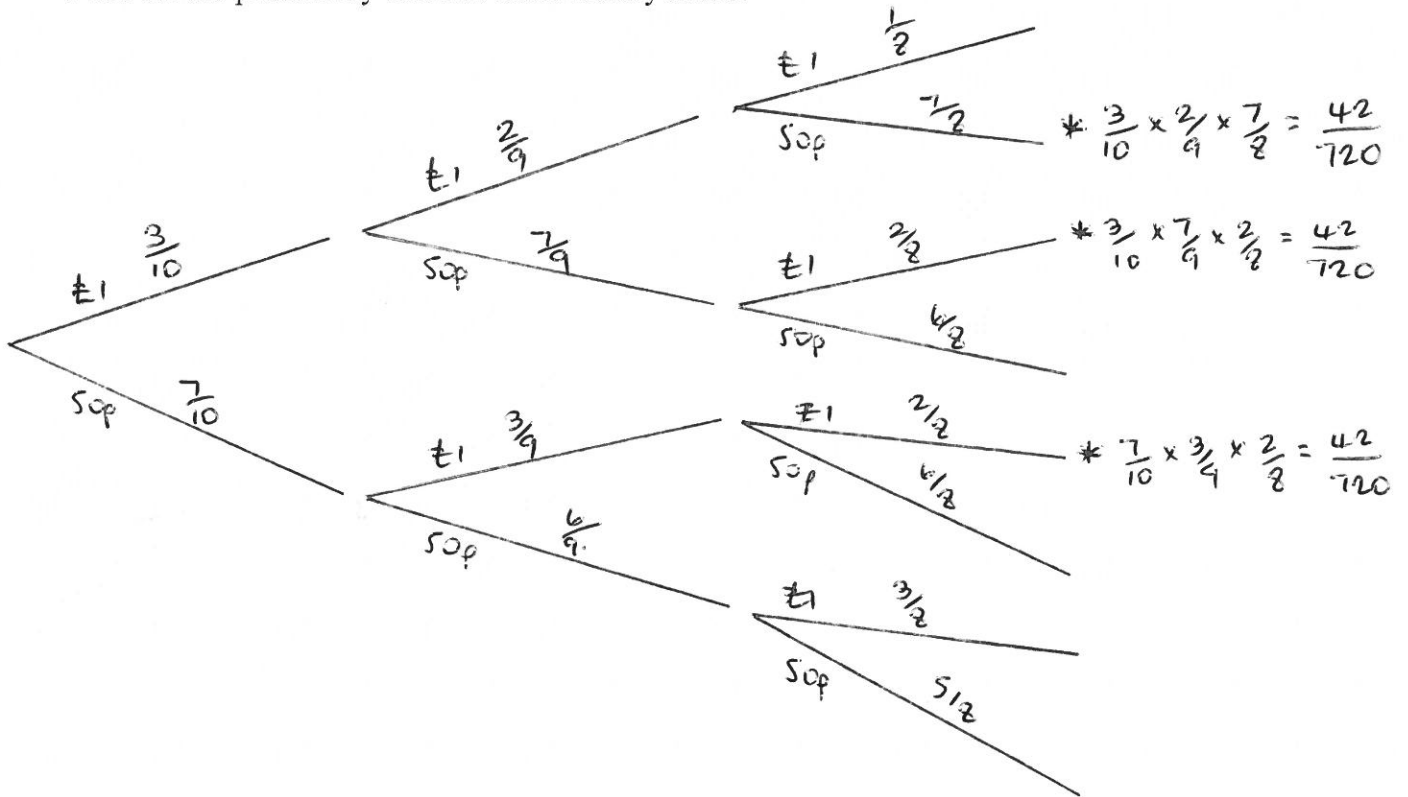
$$\dots\dots\dots 2n^2 - 1 \dots\dots\dots (3)$$

(Total 5 marks)

15. Fiza has 10 coins in a bag.
There are three £1 coins and seven 50 pence coins.

Fiza takes at random, 3 coins from the bag.

Work out the probability that she takes exactly £2.50.



$$\frac{42}{720} + \frac{42}{720} + \frac{42}{720} = \frac{126}{720}$$

$$\frac{126}{720}$$

(Total 4 marks)

16. M is directly proportional to L^3 .

When $L = 2$, $M = 160$

Find the value of M when $L = 3$

$$M \propto L^3$$

$$\therefore M = kL^3$$

$$160 = k \times 2^3 = 8k$$

$$\therefore k = \frac{160}{8} = 20$$

$$\therefore M = 20L^3$$

$$\begin{aligned} L = 3 \quad M &= 20 \times 3^3 \\ &= 20 \times 27 \\ &= 540. \end{aligned}$$

.....
540

(Total 4 marks)

17. Solve $(x-1)^2 - 2(x-1) - 3 = 0$

$$(x-1)^2 = (x-1)(x-1) = x^2 - 2x + 1$$

$$x^2 - 2x + 1 - 2x + 2 - 3 = 0$$

$$x^2 - 4x = 0 \quad \therefore x(x-4) = 0$$

$$~~(x-2)(x-2) = 0~~ \quad x = 0, 4,$$

$$\therefore \del{x=2}$$

$$x = \del{2} 0, 4$$

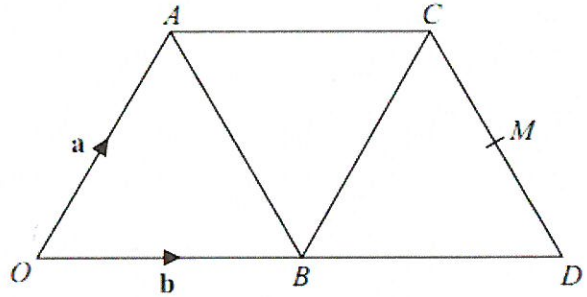
(Total 4 marks)

18. $OACD$ is a trapezium made from three equilateral triangles.

$$\vec{OA} = \mathbf{a}$$

$$\vec{OB} = \mathbf{b}$$

M is the midpoint of CD .



(a) Write \vec{AB} in terms of \mathbf{a} and \mathbf{b} .

$$\vec{AB} = -\mathbf{a} + \mathbf{b} \quad (1)$$

(b) Show that \vec{OC} is parallel to \vec{BM} .

$$\vec{OC} = \vec{OA} + \vec{AC} = \mathbf{a} + \vec{OB} = \mathbf{a} + \mathbf{b}$$

$$\begin{aligned} \vec{BM} &= \vec{BC} + \vec{CM} = \vec{OA} + \frac{1}{2} \vec{CD} = \mathbf{a} + \frac{1}{2} \vec{AB} \\ &= \mathbf{a} + \frac{1}{2} (-\mathbf{a} + \mathbf{b}) \end{aligned}$$

$$= \mathbf{a} - \frac{1}{2} \mathbf{a} + \frac{1}{2} \mathbf{b}$$

$$= \frac{1}{2} \mathbf{a} + \frac{1}{2} \mathbf{b}$$

$$= \frac{1}{2} (\mathbf{a} + \mathbf{b})$$

$$\therefore \vec{BM} = \frac{1}{2} \vec{OC}$$

$\therefore \vec{OC}$ IS PARALLEL TO \vec{BM} .

(4)

(Total 5 marks)

19. Prove algebraically that the sum of the squares of two consecutive integers is always an odd number.

LET THE 2 INTEGERS BE $n, n+1$

$$\begin{aligned}\therefore \text{SUM OF SQUARES} &= n^2 + (n+1)^2 \\ &= n^2 + n^2 + 2n + 1 \\ &= 2n^2 + 2n + 1 \\ &= 2(n^2 + n) + 1\end{aligned}$$

SINCE $2(n^2 + n)$ IS A MULTIPLE OF 2
IT IS EVEN

$\therefore 2(n^2 + n) + 1$ IS ODD

QED

(Total 3 marks)

20. Given that $\frac{8-\sqrt{18}}{\sqrt{2}} = a + b\sqrt{2}$, where a and b are integers,

find the value of a and the value of b .

$$\begin{aligned}\frac{8-\sqrt{18}}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} &= \frac{8\sqrt{2}-\sqrt{36}}{2} = \frac{8\sqrt{2}-6}{2} \\ &= 4\sqrt{2}-3 \\ &= -3 + 4\sqrt{2}\end{aligned}$$

$$a = \underline{-3}$$

$$b = \underline{4}$$

(Total 3 marks)

TOTAL FOR PAPER IS 80 MARKS