

GCSE Mathematics

Practice Tests: Set 4

Paper 3H (Calculator)

Time: 1 hour 30 minutes

You should have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator.

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- **Calculators may be used.**
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must **show all your working out.**



Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1. Here is a list of ingredients needed to make 20 cookies.

<p style="text-align: center;">Cookies</p> <p style="text-align: center;">Ingredients to make 20 cookies.</p> <p style="text-align: center;">250 g butter 120 g caster sugar 300 g flour</p>
--

Sam is going to make some cookies.

She has these ingredients.

625 g butter

360 g caster sugar

1000 g flour

Work out the greatest number of cookies that Sam can make with her ingredients.
You must show your working.

$$\text{BUTTER : } \frac{625}{250} = 2.5$$

$$\text{SUGAR : } \frac{360}{120} = 3$$

$$\text{FLOUR : } \frac{1000}{300} = 3.3\dots$$

∴ BUTTER IS LIMITING FACTOR

∴ CAN MAKE $2.5 \times 20 = 50$

50

(Total 3 marks)

2. Celina and Zoe both sing in a band.

One evening the band plays for 80 minutes.

Celina sings for 65% of the 80 minutes.

$$0.65 \times 80 = 52$$

Zoe sings for $\frac{5}{8}$ of the 80 minutes.

$$\frac{5}{8} \times 80 = 50$$

Celina sings for more minutes than Zoe sings.

Work out for how many more minutes.

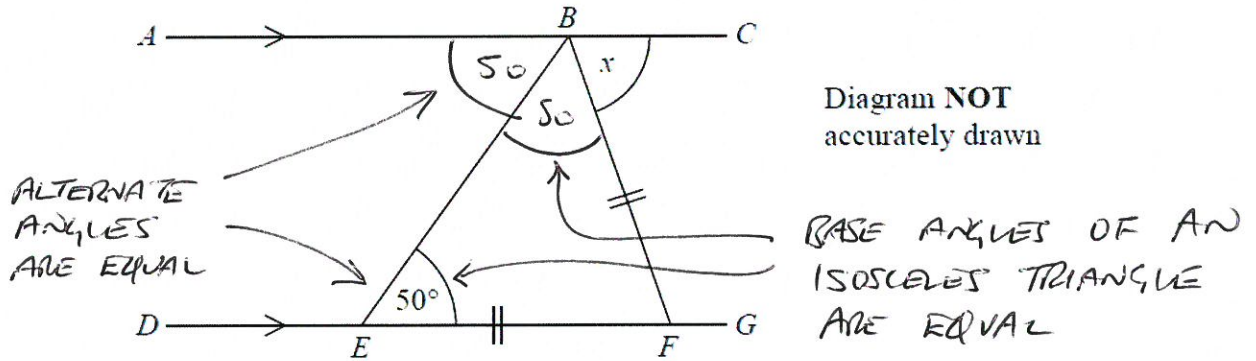
You must show all your working.

$$52 - 50 = 2$$

.....2.....minutes

(Total 4 marks)

3.



ABC is a straight line.
 $DEFG$ is a straight line.
 AC is parallel to DG .
 $EF = BF$.
Angle $BEF = 50^\circ$.

Work out the size of the angle marked x .
Give reasons for your answer.

ANGLES ON A STRAIGHT LINE ADD UP TO 180°

$$\therefore x = 180 - 50 - 50 = 80$$

80

(Total 4 marks)

4. (a) Simplify $(c^2k^5)^4$

$$\frac{c^8 k^{20}}{\dots\dots\dots} \quad (1)$$

- (b) Expand and simplify $(3x + 5)(4x - 1)$

$$12x^2 - 3x + 20x - 5$$

$$\frac{12x^2 + 17x - 5}{\dots\dots\dots} \quad (2)$$

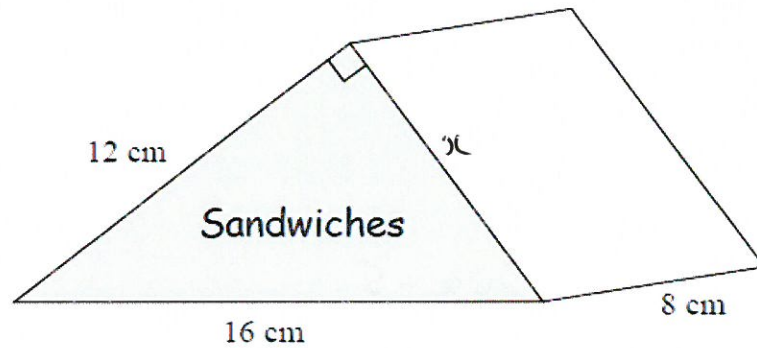
- (c) Solve $x^2 - 3x - 10 = 0$

$$(x + 2)(x - 5) = 0$$

$$x = \frac{-2, 5}{\dots\dots\dots} \quad (3)$$

(Total 6 marks)

5. Here is a sandwich packet.



The packet is in the shape of a triangular prism.
The triangular faces are right-angled triangles.

Find the volume of the sandwich packet.

$$x^2 = 16^2 - 12^2 = 112$$

$$\therefore x = \sqrt{112}$$

$$\therefore \text{AREA} = \frac{1}{2} \times 12 \times \sqrt{112}$$

$$\begin{aligned} \therefore \text{VOLUME} &= \frac{1}{2} \times 12 \times \sqrt{112} \times 8 \\ &= 507.984 \end{aligned}$$

..... 508 cm³

(Total 5 marks)

6. Make p the subject of the formula $y = 3p^2 - 4$.

$$y + 4 = 3p^2$$

$$\frac{y + 4}{3} = p^2$$

$$\sqrt{\frac{y + 4}{3}} = p$$

$$p = \sqrt{\frac{y + 4}{3}}$$

(Total 3 marks)

7. There are 10 boys and 20 girls in Mrs Brook's class.
Mrs Brook gave all the class a test.

The mean mark for all the class is 60.
The mean mark for the girls is 56.

Work out the mean mark for the boys.

$$\text{NUMBER OF GIRLS} = 56 \times 20 = 1120$$

$$\text{NUMBER OF BOYS + GIRLS} = 60 \times 30 = 1800$$

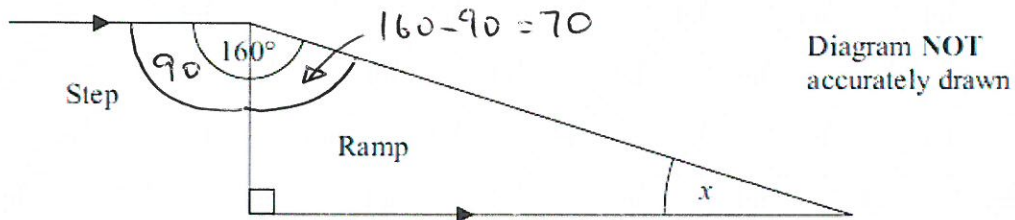
$$\therefore \text{NUMBER OF BOYS} = 1800 - 1120 = 680$$

$$\therefore \text{MEAN FOR BOYS} = \frac{680}{10} = 68$$

68

.....
(Total 3 marks)

8. The diagram shows a ramp next to a step.



- (i) Work out the size of the angle marked x .

$$x = 180 - 90 - 70 = 20$$

$$x = 20^\circ$$

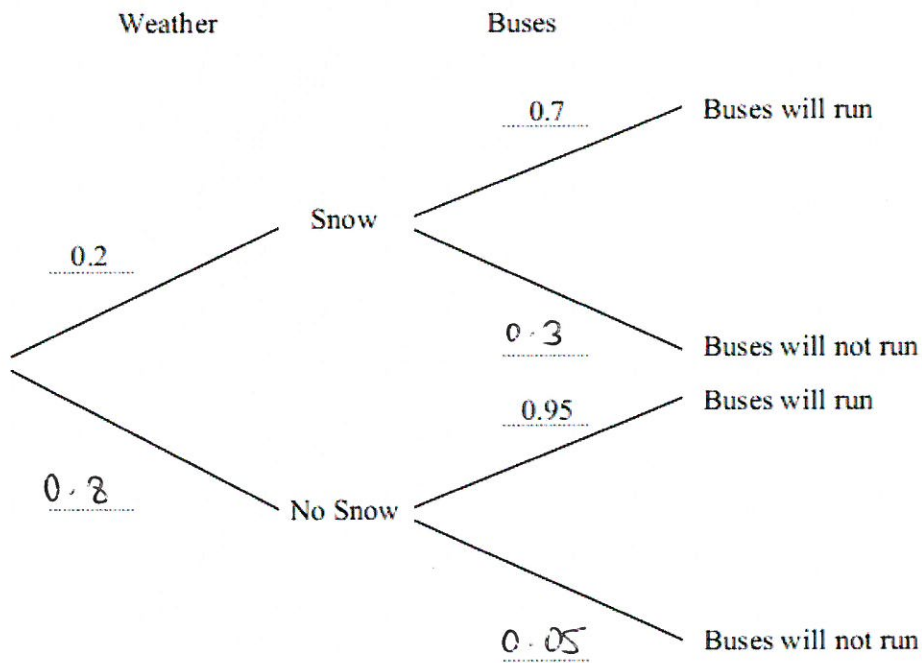
- (ii) Give a reason for your answer.

ALTERNATE ANGLES ARE EQUAL \therefore ANGLE SHOWN = 90°
ANGLES IN A TRIANGLE ADD UP TO 180°
 $\therefore x = 180 - 90 - 70 = 20$.

(Total 3 marks)

9. The decision tree diagram gives information about the probability of snow for the first 50 days in winter and the probability of whether buses will run or not run.

(a) Complete the decision tree diagram.



(2)

(b) Work out the probability that it will snow and the buses will not run.

$$0.2 \times 0.3 = 0.06$$

0.06

(2)

(Total 4 marks)

10. A baker makes jam rolls.

The baker uses flour, butter and jam in the ratio 8 : 4 : 5 to make jam rolls.

The table shows the cost per kilogram of some of these ingredients.

Cost per kilogram	
Flour	40p
Butter	£2.50
Jam	£1.00

The total weight of the flour, butter and jam for each jam roll is 425 g.

Work out the cost of these ingredients for 200 jam rolls.

	F	B	J	
	8	4	5	17
WEIGHT IN g PER ROLL	200	100	125	425 $\swarrow \times 25$
WEIGHT IN kg PER ROLL	0.2	0.1	0.125	
COST PER ROLL	$0.4 \times 0.2 = \pounds 0.08$	$2.50 \times 0.1 = \pounds 0.25$	$1 \times 0.125 = \pounds 0.125$	

$$\therefore \text{TOTAL COST PER ROLL} = 0.08 + 0.25 + 0.125 = \pounds 0.455$$

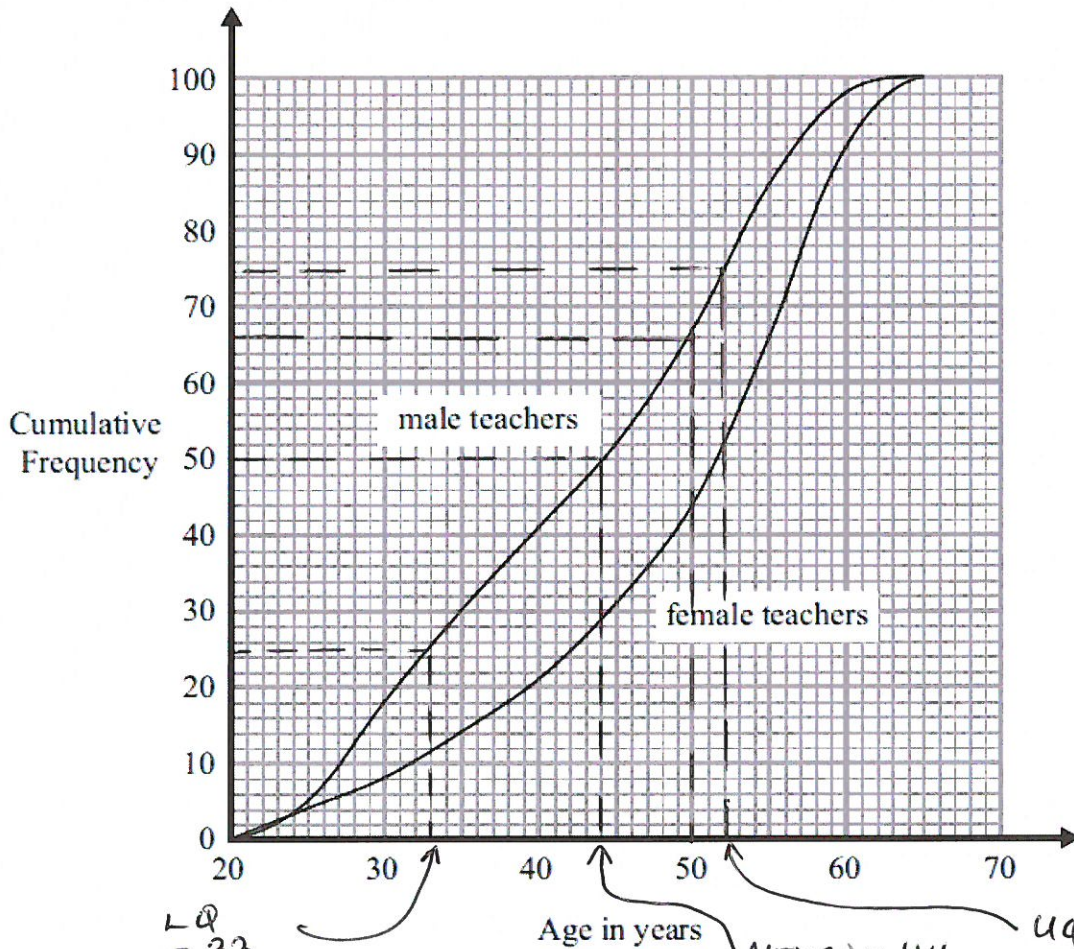
$$\therefore \text{COST FOR 200 ROLLS} = 200 \times \pounds 0.455 = \pounds 91$$

£ 91

(Total 6 marks)

11. A student did a survey of teachers' ages.

The cumulative frequency curves show information about the ages of the male teachers and the ages of the female teachers.



(a) Find an estimate for the number of the male teachers older than 50 years of age.

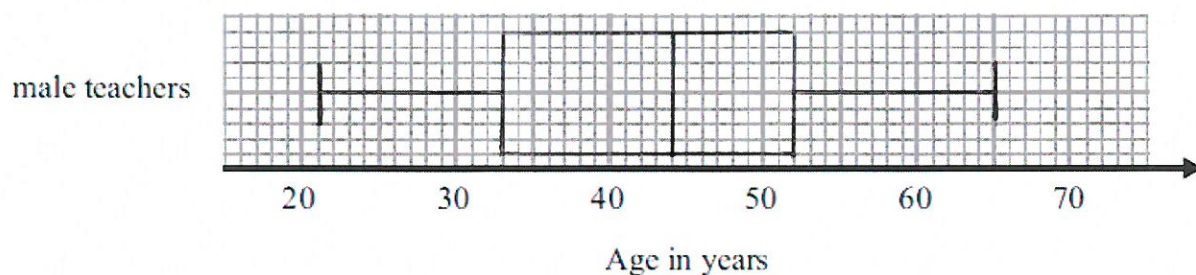
$$100 - 66 = 34$$

$$\begin{array}{r} 34 \\ \hline (32, 33 \text{ or } 34) \end{array} \quad (2)$$

The youngest male teacher was 21 years of age.

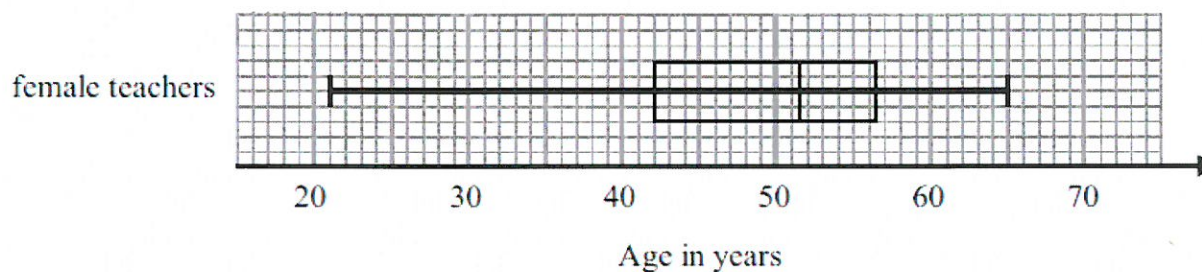
The oldest male teacher was 65 years of age.

(b) On the grid, draw a box plot to show the distribution of the ages of the male teachers.



(4)

The box plot below shows information about the ages of the female teachers.



(c) Make two comparisons between the distributions of the ages of male teachers and female teachers.

MEDIAN OF FEMALE TEACHERS (51.5) GREATER THAN MEDIAN
FOR MALE TEACHERS (44).

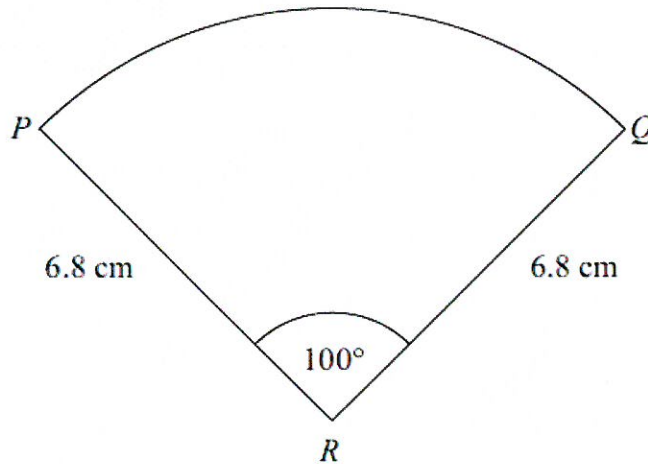
IQR FOR FEMALE TEACHERS ($56.5 - 42 = 14.5$) LESS THAN

IQR FOR MALE TEACHERS ($52 - 33 = 19$). FEMALE TEACHERS' AGES
ARE MORE CONSISTENT.

(2)

(Total 8 marks)

12. The diagram shows a sector of a circle of radius 6.8 cm.



PQ is an arc of the sector.
Angle $PRQ = 100^\circ$.

Work out the perimeter of the sector.
Give your answer correct to 3 significant figures.

$$\text{LENGTH OF ARC} = \frac{100}{360} \times 2\pi \times 6.8 = 11.9$$

$$\begin{aligned} \text{PERIMETER} &= 11.9 + 6.8 + 6.8 \\ &= 25.5 \end{aligned}$$

..... 25.5 cm

(Total 3 marks)

13. f is the function $f(x) = 2x + 5$.

(a) Find $f(3)$. $f(3) = 2 \times 3 + 5 = 11$

$$\frac{11}{\dots\dots\dots}$$

(1)

(b) Express the inverse function f^{-1} in the form $f^{-1}(x) =$

$$y = 2x + 5$$

$$y - 5 = 2x$$

$$\frac{y - 5}{2} = x$$

$$f^{-1}(x) = \frac{x - 5}{2} \dots\dots\dots$$

(2)

g is the function $g(x) = x^2 - 25$.

(c) Find $g(-3)$.

$$g(-3) = (-3)^2 - 25 \\ = 9 - 25$$

$$\frac{-16}{\dots\dots\dots}$$

(1)

(d) (i) Find $gf(x)$.

Give your answer as simply as possible.

$$gf(x) = g(2x + 5) = (2x + 5)^2 - 25 \\ = 4x^2 + 20x + 25 - 25 \\ = 4x^2 + 20x$$

$$gf(x) = 4x^2 + 20x \dots\dots\dots$$

(ii) Solve $gf(x) = 0$.

$$4x^2 + 20x = 0$$

$$\therefore x^2 + 5x = 0$$

$$\therefore x(x + 5) = 0$$

$$x = 0, -5 \dots\dots\dots$$

(5)

(Total 9 marks)

14. Dan does an experiment to find the value of π .
He measures the circumference and the diameter of a circle.

He measures the circumference, C , as 170 mm to the nearest millimetre.
He measures the diameter, d , as 54 mm to the nearest millimetre.

Dan uses $\pi = \frac{C}{d}$ to find the value of π .

Calculate the upper bound and the lower bound for Dan's value of π .

$$C_{\min} = 169.5 \quad C_{\max} = 170.5$$

$$d_{\min} = 53.5 \quad d_{\max} = 54.5$$

$$\pi_{\max} = \frac{C_{\max}}{d_{\min}} = \frac{170.5}{53.5} = 3.186915888$$

$$\pi_{\min} = \frac{C_{\min}}{d_{\max}} = \frac{169.5}{54.5} = 3.110091743$$

upper bound =3.19.....

lower bound =3.11.....

(Total 4 marks)

15. Simplify

$$\frac{x+1}{2} + \frac{x+3}{3}$$

$$\frac{3(x+1) + 2(x+3)}{6}$$

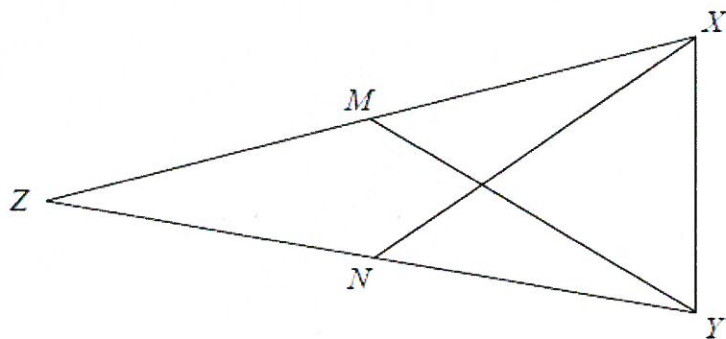
$$= \frac{3x+3 + 2x+6}{6}$$

$$= \frac{5x+9}{6}$$

$$\frac{5x+9}{6}$$

.....
(Total 3 marks)

16. The diagram shows an isosceles triangle XYZ .



$$XZ = YZ$$

M is the midpoint of XZ .

N is the midpoint of XY .

Prove that triangle XMN is congruent to triangle YNM .

Give reasons for each stage of your working.

$$XZ = YZ \quad \therefore \quad XM = YN \quad \text{SINCE } M \text{ AND } N \text{ ARE MIDPOINTS}$$

XY IS A LENGTH IN COMMON

$$\hat{N}YZ = \hat{M}XY \quad \text{SINCE BASE ANGLES IN AN ISOSCELES TRIANGLE ARE EQUAL}$$

\therefore TRIANGLES ARE CONGRUENT BY SAS

(Total 4 marks)

17. $A : B : C = x + 1 : 3 : x - 1$

$$A + B + C = 60$$

$$B = 30$$

Work out the value of x .

$$30 \div 3 = 10 \quad \therefore \text{RATIO IS MULTIPLIED UP BY 10}$$

$$\therefore 10(x + 1 + 3 + x - 1) = 60$$

$$\therefore 2x + 3 = 6$$

$$\therefore x = 1.5$$

.....
1.5

(Total 5 marks)

18. Prove that

$$(2n + 3)^2 - (2n - 3)^2 \text{ is a multiple of } 8$$

for all positive integer values of n .

$$(2n + 3)^2 = (2n + 3)(2n + 3) = 4n^2 + 12n + 9$$

$$(2n - 3)^2 = (2n - 3)(2n - 3) = 4n^2 - 12n + 9$$

$$\begin{aligned} \therefore (2n + 3)^2 - (2n - 3)^2 &= (4n^2 + 12n + 9) - (4n^2 - 12n + 9) \\ &= 4n^2 + 12n + 9 - 4n^2 + 12n - 9 \\ &= 24n \\ &= 8(3n) \\ &\text{is a MULTIPLE OF } 8 \end{aligned}$$

QED.

(Total 3 marks)

TOTAL FOR PAPER IS 80 MARKS