

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
1a	$\frac{1}{k} + \frac{2}{k} + \frac{3}{k} + \frac{4}{k} = 1 \Rightarrow k = 10$	M1 A1	1.1a 2.1	TBC
		(2)		
1b	$1 \times \frac{1}{10} + 2 \times \frac{2}{10} + 3 \times \frac{3}{10} + 4 \times \frac{4}{10} = 3$	M1 A1	1.1a 2.1	TBC
	$1^2 \times \frac{1}{10} + 2^2 \times \frac{2}{10} + 3^2 \times \frac{3}{10} + 4^2 \times \frac{4}{10} = 10$	M1 A1	1.1a 1.1b	
		(4)		
1c	$10 - 3^2 = 1$	B1	1.1b	TBC
		(1)		
1d	$E(Y) = 3 \times 3 - 2 = 7$	B1	1.1b	TBC
	$\text{Var}(Y) = 3^2 \times 1 = 9$	B1	1.1b	
		(2)		
				(9 marks)
Notes				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
2	Expectation, in points $20 \times \frac{3}{5} + -2k \times \frac{1}{5} + -4k \times \frac{1}{5} = 3$ $12 - \frac{6}{5}k = 3$ $k = 7.5$	M1 A1 M1 A1	3.3 1.1a 1.1b 2.1	TBC
(4 marks)				
Notes				
<p>Award 1st M1 for attempt to form expression for expectation in terms of k. Does not need to be equal to 3.</p> <p>Award 1st A1 for correct equation in k, unsimplified or simplified.</p> <p>Award 2nd M1 for attempt to solve <i>their</i> equation in k.</p> <p><u>Alternative method</u></p> <p>$20 - 0.2(20 + 2k) - 0.2(20 + 4k) = 3$ for 1st M1, A1 (or any scalar multiple of this equation)</p> <p>Leading to: $12 - 1.2k = 3$ as above</p>				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
3a	0.15	B1	1.2	TBC
		(1)		
3b	$E(X) =$	M1	1.1a	TBC
	$-3 \times 0.1 + -2 \times 0.2 + -1 \times 0.15 + 0 \times 0.4 + 1 \times 0.15 = -0.7$	A1	1.1b	
	$E(X^2) = 9 \times 0.1 + 4 \times 0.2 + 1 \times 0.15 + 0 \times 0.4 + 1 \times 0.15 = 2$	M1	1.1a	
	$\text{Var}(X) = 2 - (-0.7)^2 = 1.51$	A1	2.1	
		(4)		
3c	$P(X > 2Y) \Rightarrow P(X < -\frac{2}{3}) = 0.1 + 0.2 + 0.15 = 0.45$	M1 A1	3.1a 1.1b	TBC
		(2)		
				(7 marks)
Notes				
3b, Allow follow through from incorrect part a for all M marks.				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
4a	$2k + 3k + 3k + 4k = 1 \Rightarrow 12k = 1 \Rightarrow k = \frac{1}{12}$	M1 A1	1.1a 2.1	TBC
		(2)		
4b	$E(X) = 1 \times \frac{2}{12} + 2 \times \frac{3}{12} + 4 \times \frac{3}{12} + 5 \times \frac{4}{12} = \frac{40}{12} = \frac{10}{3}$	M1 A1	1.1a 1.1b	TBC
	$E(X^2) = 1 \times \frac{2}{12} + 4 \times \frac{3}{12} + 16 \times \frac{3}{12} + 25 \times \frac{4}{12} = \frac{27}{2}$ $\text{Var}(X) = \frac{27}{2} - \left(\frac{10}{3}\right)^2 = \frac{43}{18}$	M1 A1	1.1a 1.1b	
		(4)		
4c	$(-4)^2 \times \frac{43}{18} = \frac{344}{9}$	M1 A1	1.2 2.1	TBC
		(2)		
(8 marks)				
Notes				
<p>4b Allow follow through from <i>their</i> k for M marks.</p> <p>4c Allow follow through from their $\text{Var}(X)$ for M mark.</p>				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
5a	$a + b = 0.4$ $E(Y) = -5 \times 0.2 + -3 \times 0.1 + a + 5b + 7 \times 0.3 = 2.4$ $\Rightarrow a + 5b = 1.6$ $a = 0.1, b = 0.3$	B1 M1 M1 A1 A1	1.1b 3.1a 1.1b 1.1b 1.1b	TBC
		(5)		
5b	$E(X^2) = 1 \times 0.2 + 0 \times 0.1 + 4 \times 0.1 + 16 \times 0.3 + 25 \times 0.3 = 12.9$ $E(X) = 2.7$ $\text{Var}(X) = 12.9 - 2.7^2 = 5.61$	M1 M1 A1	1.1a 1.1b 2.1	TBC
		(3)		
5c	22.44	B1ft	1.1b	TBC
		(1)		
5d	$P(X - 3 > 2Y) = P(X < 1) = 0.3$	M1 A1	3.1a 1.1b	TBC
		(2)		
(11 marks)				
Notes				
<p>5a</p> <p>1st M1 for attempt to find Y_s.</p> <p>2nd M1 for attempt to form equation for $E(Y)$.</p> <p>5c</p> <p>Allow follow through from b.</p>				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
6a	$-1.7 = 4 - 3E(X) \Rightarrow E(X) = 1.9$ $-1 \times a + 0 \times b + 1 \times a + 2 \times b + 3 \times a + 4 \times c = 1.9$ $\Rightarrow 3a + 2b + 4c = 1.9$ [1] (or scalar multiple of this equation, e.g. $9a + 6b + 12c = 5.7$) $P(Y < 0)$ gives $P(X > 2)$ hence $a + b + c = 0.6$ [2] $3a + 2b + c = 1$ [3] Solve system using matrices or elimination: $a = 0.1, b = 0.2, c = 0.3$	M1 M1	3.1a 1.1b	TBC
	M1 M1 M1 A1 A1	2.1 1.1b 1.1b 1.1b 1.1b		
		(7)		
6b	$27.81 \div 9 = 3.09$	M1 A1	1.1a 1.2	TBC
		(2)		
6c	$P(X < Y)$ means $P(X < 1)$ $P(X < 1) = 0.1 + 0.2 = 0.3$	M1 A1ft	3.1a 1.1b	TBC
		(2)		
(11 marks)				
Notes				
6a 1 st A1 for any two of a, b and c correct. 6c Allow follow through from <i>their</i> a and b .				