1 The discrete random variable *X* has a probability distribution function

$$P(X = x) = \frac{x}{k}$$
 x = 1, 2, 3, 4

where k is a constant.

a	Show that $k = 10$.	(2 marks)
b	Show that $E(X) = 3$ and find the value of $E(X^2)$.	(4 marks)
c	Calculate the variance of <i>X</i> .	(1 mark)
Tł	he random variable $Y = 3X - 2$	

d Find E(Y) and Var(Y).

2 Caitlin is designing a game of chance for her school fete.

She has a fair, five-sided spinner marked with the numbers 1, 2, 3, 4 and 5.

Players get 20 virtual points to have a go at spinning an even number.

If they are successful, they win their points back plus k times the number spun.

Points won can then be exchanged for small prizes.

Given that Caitlin's expected winnings per game is 3 points, show that k = 7.5. (4 marks)

3 The discrete random variable *X* has a probability distribution given in the table below.

x	-3	-2	-1	0	1
$\mathbf{P}(X=x)$	0.1	0.2	k	0.4	0.15

Table 1

a Write down the value of *k*.

b Find the expectation of *X* and show that Var(X) = 1.51.

The random variable Y = 2X + 1.

c Find
$$P(X > 2Y)$$
. (2 marks)

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(2 marks)

(1 mark)

(4 marks)

4 The discrete random variable *X* has a probability distribution function

$$P(X = x) = \begin{cases} k(x+1) & x = 1, 2\\ k(x-1) & x = 4, 5 \end{cases}$$

a Show that $k = \frac{1}{12}$ (2 marks)

(4 marks)

(1 mark)

(2 marks)

- **b** Find the exact values of E(X) and Var(X).
- **c** Show that $Var(2-4X) = \frac{344}{9}$ (2 marks)
- 5 The discrete random variable *X* has a probability distribution given in the table below.

Table 2					
x	-1	0	2	4	5
$\mathbf{P}(X=x)$	0.2	0.1	a	b	0.3

The random variable *Y* is defined as Y = 2X - 3.

Given that E(Y) = 2.4,

- **a** Find the values of a and b.(5 marks)**b** Calculate $E(X^2)$ and show that Var(X) = 5.61.(3 marks)
- **c** Write down the value of Var(*Y*).
- **d** Find P(X 3 > 2Y).

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6 The discrete random variable *X* has a probability distribution given by

			Table 3			
x	-1	0	1	2	3	4
$\mathbf{P}(X=x)$	а	b	а	b	а	С

The random variable *Y* is defined as Y = 4 - 3X.

Given that E(Y) = -1.7 and the P(Y < 0) = 0.6,

a Calculate the values of a, b and c.(7 marks)Given that Var(Y) = 27.81,(2 marks)b Find the exact value of Var(X).(2 marks)c Find P(X < Y).(2 marks)

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