

## Pure 18 – Trigonometry

Please **complete** this homework by \_\_\_\_\_. Start it early. If you can't do a question you will then have time to ask your teacher for help or go to a drop in session.

### Section 1 – Review of previous topics. Please complete all questions.

1. Find the following indefinite integrals.

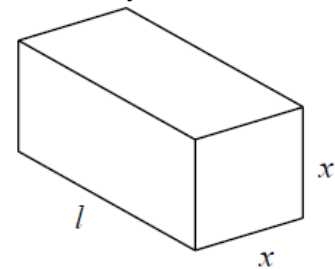
a)  $\int (6x^2 + 2)dx$    b)  $\int x^{\frac{1}{3}}dx$    c)  $\int (2 + \sqrt{x})dx$    d)  $\int 4x^{-3}dx$    e)  $\int \frac{3}{x^2}dx$ .

2. a) Express  $x\sqrt{x}$  in the form  $x^k$ , where  $k$  is a constant.

b) Hence find  $\int x\sqrt{x}dx$

3. Evaluate a)  $\int_1^8 x^{-\frac{1}{3}}dx$    b)  $\int_1^4 6\sqrt{x}dx$

4. The diagram shows a square prism of length  $l$  cm and cross section  $x$ cm by  $x$ cm. Given that the surface area of the prism is  $36\text{cm}^2$ ,



a) Write down an equation for the surface area of the prism

b) show that  $l = \frac{18 - x^2}{2x}$

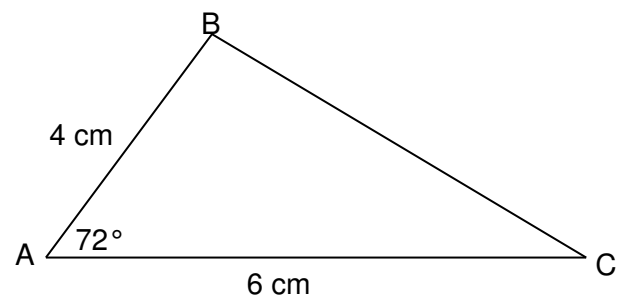
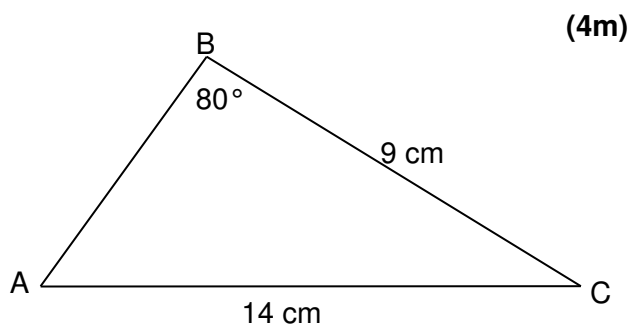
c) Find the value of  $x$  for which the volume is a maximum and hence the value of  $l$

### Section 2 – Consolidation of this week's topic. Please complete all questions.

1. Use the sine rule to find the value of angle A.

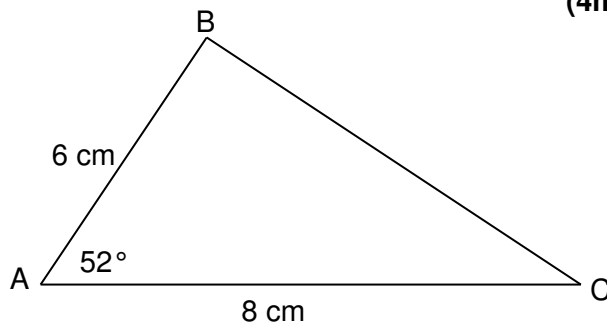
2. Calculate the area of the triangle.

**(2m)**



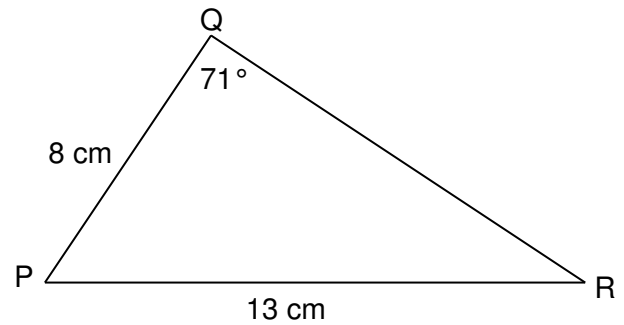
3. Use the cosine rule to find the length of BC.

(4m)



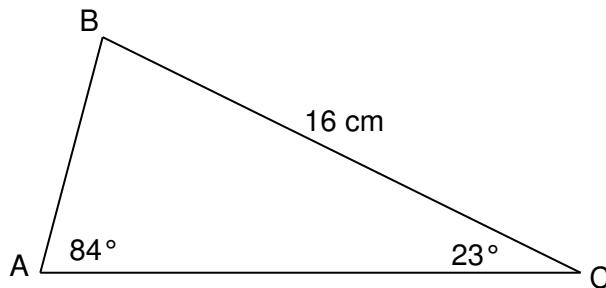
4. Find the size of angle R

(4m)



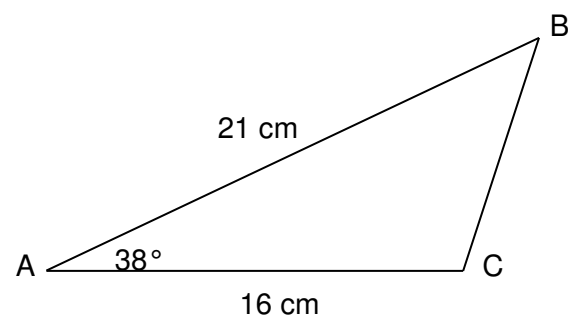
5. Calculate the length of AB.

(3m)



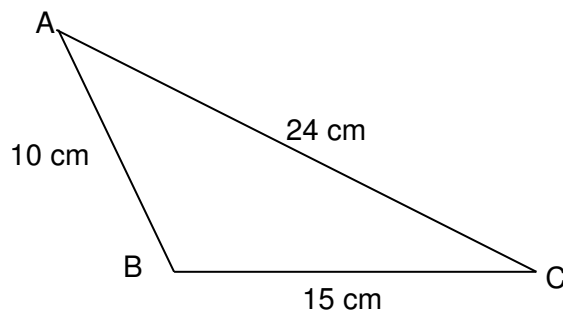
6. Calculate the length of BC.

(4m)



7. Calculate the size of angle B

(4m)



8. In the triangle ABC, angle A =  $40^\circ$ ,  
angle B =  $75^\circ$  and AB = 6 cm.

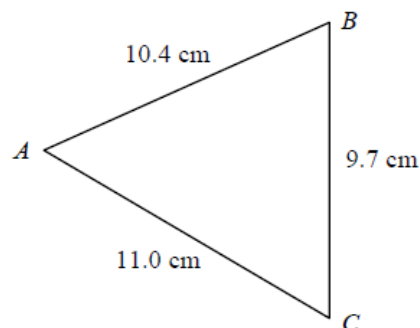
a) Calculate the length of AC

(3m)

b) Find the area of the triangle.

(2m)

9.



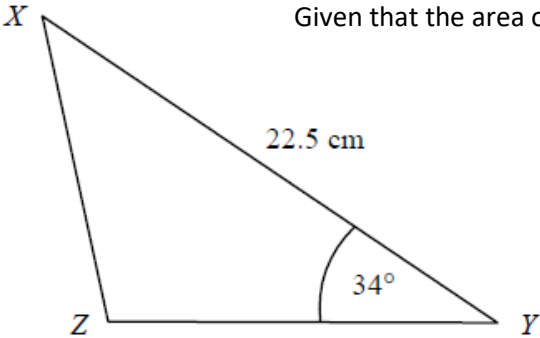
Find the area of the triangle ABC to 3  
significant figures.

(6m)

(Total 36 marks)

Section 3 – Extension questions. If you are aiming for a top grade, you should attempt these questions.

1. Joanne walks 4.2km on a bearing of  $138^\circ$ . She then walks 7.8km on a bearing of  $251^\circ$ .
  - a. Calculate how far Joanne is from where she started. **(4m)**
  - b. Find as a bearing, the direction in which Joanne would have to walk in order to return to the point where she started. **(4m)**
  
2. A ferry and a cargo ship are both approaching the same port. The ferry is 3.2km from the port on a bearing of  $076^\circ$  and the cargo ship is 6.9km from the port on a bearing of  $323^\circ$ .  
Find the distance between the 2 vessels and the bearing of the cargo ship from the ferry. **(8m)**

3.  Given that the area of the triangle is  $100\text{cm}^2$ , find the length XZ **(4m)**