

## Pure 26 – Differentiation: Trig, Exponentials, Logs & Chain Rule

Please <u>complete</u> this homework by \_\_\_\_\_\_. Start it early. If you can't do a question you will then have time to ask your teacher for help or go to a drop in session.

## Section 1 – Review of previous topics. Please <u>complete</u> all questions.

- 1. Differentiate these functions:
  - a)  $y = 3x^2$ b)  $y = x^3 + 5$ c)  $y = x^5 + 4x^3 + 2x$ d) f(x) = 5e) f(x) = 2xe)  $f(x) = x(x^3 + 4)$

## 2. Differentiate these functions:

a)	$f(x) = \sqrt{x}$	b) $f(x) = 6x^{-2}$	c) $f(x) = x + \frac{1}{x}$
d)	$y = x^{\frac{2}{3}} + x^{\frac{5}{3}}$	e) $y = x^2 - \frac{8}{x^2}$	f) $y = \frac{2x^3 + 3x}{\sqrt{x}}$

- 3. Prove from first principles that the derivative of  $x^2$  is 2x.
- 4. Find the equation of the tangent to the curve  $y = 2x^3 + 6x + 10$  at the point (-1,2).
- 5. Find the coordinates of the point where the tangent to the curve  $y = x^2 + 1$  at the point (2,5) meets the normal to the same curve at the point (1,2).
- 6. Simplify  $\sqrt{75} \sqrt{12}$  giving your answer in the form  $a\sqrt{b}$  where a and b are integers to be found.
- 7. Write  $2 + 0.8x 0.04x^2$  in the form  $A B(x + C)^2$ .
- 8. Given that the function  $f(x) = sx^2 + 8x + s$  has equal roots, find the value of the positive constant s.
- 9. Given that the simultaneous equations y x = k and  $x^2 + y^2 = 4$  have exactly one pair of solutions, show that  $k = \pm 2\sqrt{2}$ .
- 10. Find the set of values of x for which  $x^2 5x 14 > 0$ . Write your answer using set notation.



## Section 2 – Consolidation of this week's topic. Please <u>complete</u> all questions.

- 1) Differentiate with respect to x and simplify where possible: a)  $y = 2 \cos x$  b)  $f(x) = \sin 4x$  c)  $y = 5 \sin(\frac{\pi x}{3})$ d)  $f(x) = 3\sin 2x + 5\cos x$  e)  $y = \frac{3x^4 + 2x\sin x}{x}$  [7]
- **2)** Prove from first principles that the derivative of  $\cos 3x$  is  $-3\sin 3x$ . **[5]**
- 3) A curve has the equation  $y = x + \cos x$ . Find the equation of the tangent to the curve at  $x = \frac{\pi}{6}$ , leaving your answer exact. [4]
- 4) Differentiate with respect to x and simplify where possible: a)  $y = e^{3x}$  b)  $f(x) = e^{-2x} + \ln 3x$  c)  $y = 5^x$ d)  $f(x) = \ln 4x^5$  e)  $y = 2^{3x-1}$  [9]
- 5) A curve has the equation  $y = \ln x + \frac{3}{x}$ . Find the equation of the normal to the curve at x = 1, leaving your answer exact. [5]
- 6) Differentiate with respect to x and simplify where possible: a)  $y = (3 + 2x)^5$  b)  $f(x) = (3 - 2x)^{-4}$  c)  $y = (2 + 3x^2)^3$ d)  $f(x) = (x^2 + 3x + 1)^5$  e)  $y = 5(x^2 - 1)^{\frac{1}{2}}$  [15]
- 7) A curve has the equation  $y = (e^x + \ln x)^2$ . Find the equation of the tangent to the curve at x = 1, leaving your answer exact. [5]
- 8) The curve with equation  $y = 4 e^x$  meets the y axis at point P and the x axis at point Q.
  - a) Find the equation of the normal to the curve at P.
  - b) Find the equation of the tangent to the curve at Q.

The normal to the curve at P meets the tangent to the curve at Q at the point R. The x coordinate of R is  $a \ln 2 + b$  where a and b are rational constants.

c) Show that  $a = \frac{8}{5}$ . d) Find the value of b. [10]

Total: 60 Marks